CASTOR: Programming with Extensible Generative Visitors

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Abstract

Much recent work on type-safe extensibility for Object-Oriented languages has focused on design patterns that require modest type system features. Examples of such design patterns include *Object Algebras, Extensible Visitors, Finally Tagless interpreters*, or *Polymorphic Embeddings*. Those techniques, which often use a functional style, can solve basic forms of the Expression Problem. However, they have important limitations.

This paper presents CASTOR: a Scala framework for programming with extensible, generative visitors. CASTOR has several advantages over previous approaches. Firstly, CASTOR comes with support for (type-safe) pattern matching to complement its visitors with a concise notation to express operations. Secondly, CASTOR supports type-safe interpreters (à la Finally Tagless), but with additional support for pattern matching and a generally recursive style. Thirdly, CASTOR enables many operations to be defined using an imperative style, which is significantly more performant than a functional style (especially in the JVM platform). Finally, functional techniques usually only support tree structures well, but graph structures are poorly supported. CASTOR supports type-safe extensible programming on graph structures. The key to CASTOR's usability is the use of annotations to automatically generate large amounts of boilerplate code to simplify programming with extensible visitors. To illustrate the applicability of CASTOR we present several applications and two case studies. The first case study compares the ability of CASTOR for modularizing the interpreters from the "Types and Programming Languages" book with previous modularization work. The second case study on UML activity diagrams illustrates the imperative aspects of CASTOR, as well as its support for hierarchical datatypes and graphs.

Keywords: modularity, visitor pattern, pattern matching, metaprogramming, OOP

1. Introduction

5

For many years researchers have been looking at improving modularity mechanisms in programming languages. A particular problem that is the focus of much recent work in modularity is the so-called Expression Problem [1]. In the Expression Problem, the key challenge is how to achieve *type-safe extensibility*. That is, how to: evolve software

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in two dimensions (adding new variants and operations) without rewriting existing code; and without using type-unsafe features (such as casts or reflection). Over the years, many solutions were proposed. Some work proposes new programming languages or programming language features designed specifically with modularity in mind. These

- include virtual classes [2], multi-methods [3], and family polymorphism [4]. Other work has focused on more general language features such as generics [5], higher-kinded types [6], virtual types [7], traits [8] and mixins [5] which can also help with various modularity problems.
- Much of the more recent work on type-safe extensibility for Object-Oriented languages focus is on design patterns that require modest type system features. Examples of such design patterns include *Object Algebras* [9], *Modular Visitors* [10], *Finally Tagless interpreters* [11] or *Polymorphic Embeddings* [12]. All of those techniques can solve basic forms of the Expression Problem, and are closely related.

The foundation for a lot of that work comes from functional programming and type-theoretic encodings of datatypes [13, 14]. In particular, the work by Hinze [15] was the precursor for those techniques. In his work Hinze employed so-called Church [13] and Scott [14] encodings of datatypes to model generic programming libraries. Later Oliveira et al. [16, 17] showed that variants of those techniques have wider applications and solve the Expression Problem [1]. These ideas were picked up by Carrete et al. [11]

- to enable tagless interpreters, while also benefited from the extensibility properties of the techniques. Carrete et al.'s work popularized those applications of the techniques as the nowadays so-called *Finally Tagless* style. Soon after Hofer et al. [12] proposed *Polymorphic Embeddings* in Scala, highly inspired by the Finally Tagless style in languages like Haskell and OCaml.
- ³⁰ In parallel with the work on *Finally Tagless* and *Polymorphic Embeddings* the connections of those techniques to the VISITOR pattern in OOP were further explored [18], building on observations between the relationship between type-theoretic encodings of datatypes and visitors by Buchlovsky and Thielecke [19]. That work showed that Church and Scott encodings of datatypes correspond to two variants of the VISITOR pattern called,
- respectively, *Internal* and *External* visitors. Later on Oliveira and Cook [9] showed a simplified version of *Internal Visitors* called *Object Algebras*, which could solve the Expression Problem even in languages like Java.

While Internal Visitors, Object Algebras, Finally Tagless or Polymorphic Embeddings can all be traced back to Church encodings, there has been much less work on

- techniques that are based on Scott encodings. Scott encodings are more powerful, as they allow a (generally) recursive programming style. In contrast, Church encodings rely on a programming style that is akin to programming with folds in functional programming [20]. In general, Scott encodings require more sophisticated type system features, which is one reason why they have seen less adoption. In particular recursive
- ⁴⁵ types are necessary, which also brings up extra complications due to the interaction of recursive types and subtyping. Nevertheless, recent work by Zhang and Oliveira [21] on the Java EVF framework picked up on modular *External Visitors* and shows *External Visitors* can be made practical even with modest language features and code generation. The applicability of EVF is demonstrated by refactoring interpreters from the "Types"
- ⁵⁰ and Programming Languages" (TAPL) book [22]. The interpreters are modularized, and various specific interpreters are recovered from modular, reusable components. This

effort is non-trivial because TAPL interpreters are written in a small-step operational semantics style, which does not fit well with folds. The fundamental problem is that the recursion pattern for small-step operational semantics is quite different from a fold.

- ⁵⁵ Furthermore, many operations employed by implementations of TAPL interpreters depend on other operations. Such *dependencies* are hard to model in a modular setting, but the use of EVF's *External Visitors* can account for them. However, there are still critical limitations on existing type-safe extensibility approaches, including EVF. One drawback is the lack of support for pattern matching, which makes writing various oper-
- ations quite cumbersome. Another drawback is that even for the techniques that have been adapted to Object-Oriented Programming (OOP), the focus is still on a functional programming style. Writing operations in an imperative style is difficult, and supporting graph structures (which are common in OOP) is nearly impossible.

This paper presents CASTOR: a Scala framework for programming with extensible,

⁶⁵ generative visitors. Unlike previous work, CASTOR aims to support not only a functional style but also an imperative programming style with visitors. CASTOR visitors bring several advantages over existing approaches:

Concise Notation. Programming with the VISITOR pattern is typically associated with a lot of boilerplate code. *Extensible Visitors* make the situation even worse due to the heavy use of sophisticated type system features. Although previous work on EVF alleviated the burden of programmers by generating boilerplate code related to visitors and traversals, it is restricted by Java's syntax and annotation processor. CASTOR improves on EVF by employing Scala's concise syntax and Scalameta¹ to simplify client code. Unlike the Java annotation processor which generates code separately, Scalameta enables

⁷⁵ direct transformation on the client code, further reducing the boilerplate and hiding sophisticated type system features from users.

Pattern Matching Support. CASTOR comes with support for (type-safe) pattern matching to complement its visitors with a concise notation to express operations. In the OOP context, data structures are open. However, the traditional semantics of pattern matching

- ⁸⁰ adopted by many approaches is based on the *order* of patterns, which conflicts with the openness of OO data structures. Therefore, we suggest that a more restricted, top-level pattern matching model, where the order of patterns is irrelevant. To compensate for the absence of ordered patterns we propose a complementary mechanism for case analysis with defaults, which can be used when nested or multiple case analysis is needed.
- ⁸⁵ CASTOR adopts this new pattern matching model. As a result, pattern matching in CASTOR is concise, exhaustive, extensible and composable.

GADT-Style Definitions. CASTOR supports type-safe interpreters (à la *Finally Tagless*), but with additional support for pattern matching and a generally recursive style. While *Finally Tagless* interpreters are nowadays widely used by programmers in multiple

⁹⁰ languages (including Haskell and Scala), they must be written in fold-like style. Supporting operations that require nested patterns, or simply depend on other operations is

¹http://scalameta.org

quite cumbersome (although workarounds exist [23]), especially if modularity is to be preserved. In contrast, CASTOR can support those features naturally.

Hierarchical Datatypes. Functional datatypes are typically flat where variants have no relationship with each other. Object-oriented style datatypes, on the other hand, can be hierarchical [24] where datatype constructors can be refined by more specific constructors. Hierarchical datatypes facilitate reuse since the subtyping relation allows the semantics defined for supertypes to be reused for subtypes. CASTOR exploits OOP features and employs subtyping to model hierarchical datatypes.

Imperative Traversals. CASTOR enables many operations to be defined using an imperative style, which is significantly more performant than a functional style (especially in the JVM platform). Both functional and imperative visitors [19] written with CASTOR are fully extensible and can later support more variants modularly. Imperative visitors enable imperative style traversals that instead of returning a new Abstract Syntax Tree (AST), modify an existing AST in-place.

Graph Structures. Finally functional techniques usually only support tree structures well, but graph structures are poorly supported. CASTOR supports type-safe extensible programming on graph structures. Compared to trees, graphs are a more general data structure that have many important applications such as common subexpression elimination.

- In summary, this paper makes the following contributions:
- Extensible pattern matching with modular external visitors: We evaluate existing approaches to pattern matching in an OOP context (Section 2). We show how to incorporate extensible (or open) pattern matching support on modular external visitors, which allows CASTOR to define non-trivial pattern matching operations.
- **Support for hierarchical datatypes:** Besides flat datatypes that are typically modeled in functional languages, we show how OOP style hierarchical datatypes are supported in CASTOR (Section 3).
- **Support for GADTs:** We show how to use CASTOR'S support for GADTs in building well-typed interpreters (Section 4), which would be quite difficult to model in a *Finally Tagless* style.
 - **Imperative style modular external visitors:** We show how to define imperative style modular external visitors in CASTOR (Section 5).
- **Support for graph structures:** We show how to do type-safe extensible programming on graph structures, which generalize the typical tree structures in functional programming (Section 5).
 - **The CASTOR framework:** We present a novel encoding for modular pattern matching based on extensible visitors (Section 2.7). The encoding is automated using metaprogramming and the transformation is formalized (Section 6).

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- **Case studies:** We conduct two case studies to illustrate the effectiveness of CASTOR. The first case study on TAPL interpreters (Section 7) demonstrates functional aspects of CASTOR, while the second one on UML activity diagrams (Section 8) demonstrates the object-oriented aspects of CASTOR.
- This paper is a significantly extended version of a conference paper [25]. We revise the presentation of the paper and more importantly extend CASTOR with novel features. Firstly, we add a detailed comparison with our previous work on EVF (Section 2.8). Secondly, we improve the way of declaring variants of open datatypes, which enables hierarchical variants (Section 3), GADTs (Section 4), graphs and imperative style
 visitors (Section 5). Thirdly, we revise the formalization according to the new encoding
- (Section 6). Finally, we conduct an additional case study on UML activity diagrams (Section 8) for assessing these added features.

Source code for examples, case studies and the CASTOR framework is available at:

https://github.com/wxzh/Castor

145 2. Open Pattern Matching

Pattern matching is a pervasive and useful feature in functional languages (e.g. ML [26] and Haskell [27]) for processing data structures conveniently. Data structures are firstly modeled using algebraic datatypes and then processed through pattern matching. On the other hand, OOP uses class hierarchies instead of algebraic datatypes to model data structures. Still, the same need for processing data structures also exists in OOP. However, there are important differences between data structures modeled with algebraic datatypes and class hierarchies. Algebraic datatypes are typically *closed*, having a fixed set of variants. In contrast, class hierarchies are *open*, allowing the addition of new variants. A closed set of variants facilitates exhaustiveness checking of

- patterns but sacrifices the ability to add new variants. OO class hierarchies do support the addition of new variants, but without mechanisms similar to pattern matching, some programs are unwieldy and cumbersome to write. In this section, we first characterize four desirable properties of pattern matching in the context of OOP. We then review some of the existing pattern matching approaches in OOP and discuss why they fall in short of the desirable properties. This section ends with an overview of CASTOR and an
- ⁶⁰ short of the desirable properties. This section ends with an overview of CASTOR and an evaluation summary on the presented approaches.

2.1. Desirable Properties of Open Pattern Matching

We identify the following desirable properties for pattern matching in an OOP context:

165

- **Conciseness.** Patterns should be described concisely with potential support for wildcards, deep patterns, and guards.
- **Exhaustiveness.** Patterns should be exhaustive to avoid runtime matching failure. The exhaustiveness of patterns should be statically verified by the compiler and the missing cases should be reported if patterns are incomplete.

- **Extensibility.** Datatypes should be extensible in the sense that new data variants can be added while existing operations can be reused without modification or recompilation.
 - **Composability.** Patterns should be composable so that complex patterns can be built from smaller pieces. When composing overlapped patterns, programmers should be warned about possible redundancies.

Using these properties as criteria, we next evaluate pattern matching approaches in OOP. We show that many widely used approaches lack some of these properties. We argue that a problem is that many approaches try to closely follow the traditional semantics of pattern matching, which assumes a closed set of variants. Under a closed set of variants, it is natural to use the *order* of patterns to prioritize some patterns over the others. However, when the set of variants is not predefined a priori then relying on some ordering of patterns is problematic, especially if separate compilation and modular type-checking are to be preserved. Nonetheless, many OO approaches, which try to support both an extensible set of variants and pattern matching, still try to use the order of patterns to define the semantics. Unfortunately, this makes it hard to support other desirable properties such as exhaustiveness or composability.

2.2. Running Example: ARITH

To facilitate our discussion, a running example from TAPL [22]—an untyped, arithmetic language called ARITH—is used throughout this paper. The syntax and semantics of ARITH are formalized in Figure 1. Our goal is to model the syntax and semantics of ARITH in a concise and modular manner.

ARITH has the following syntactic forms: zero, successor, predecessor, true, false, conditional and zero test. The definition nv identifies 0 and successive application of succ to 0 as numeric values. The operational semantics of ARITH is given in *small-step*

- style, with a set of reduction rules specifying how a term can be rewritten in one step. Repeatedly applying these rules will eventually evaluate a term to a value. There might be multiple rules defined on a single syntactic form. For instance, rules PREDZERO, PREDSUCC and PRED are all defined on a predecessor term. How pred *t* is going to be evaluated in the next step is determined by the shape of the inner term *t*: if *t* is 0, then PREDZERO will be applied; if *t* is a successor application to a numeric value, then
- PredSucc will be applied; otherwise Pred will be applied.

ARITH is a good example for assessing the four properties because: 1) The small-step style semantics is best expressed with a concise *nested case analysis* on terms; 2) ARITH is, in fact, a unification of two sublanguages, NAT (zero, successor and predecessor) and

²⁰⁵ BOOL (true, false, and conditional) plus an extension (zero test). Ideally, NAT and BOOL should be *separately defined* and *modularly reused*.

2.3. The VISITOR Pattern

The VISITOR design pattern [18] is frequently used to implement interpreters or compilers because of its ability to add new interpretations or compiler phases without ²¹⁰modifying the class hierarchy. Let us implement the ARITH language using the VISITOR pattern step by step. The implementation is written in Scala without using any Scalaspecific features and can be easily mapped to other OOP languages like C++ or Java.

170

t ::= 0 | succ t | pred t | true | false | if t then t else t | iszero t nv ::= 0 | succ nv





Abstract Syntax. The abstract syntax of ARITH is modeled by the following class hierarchy:

```
abstract class Tm {
215
      def accept[A](v: TmVisit[A]): A
   }
   class TmZero() extends Tm {
      def accept[A](v: TmVisit[A]) = v.tmZero(this)
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   }
   class TmSucc(val t: Tm) extends Tm {
     def accept[A](v: TmVisit[A]) = v.tmSucc(this)
   }
   class TmPred(val t: Tm) extends Tm {
      def accept[A](v: TmVisit[A]) = v.tmPred(this)
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   }
   class TmTrue() extends Tm {
      def accept[A](v: TmVisit[A]): A = v.tmTrue(this)
   }
   class TmFalse extends Tm {
230
      def accept[A](v: TmVisit[A]): A = v.tmFalse(this)
   }
   class TmIf(val t1: Tm, val t2: Tm, val t3: Tm) extends Tm {
      def accept[A](v: TmVisit[A]): A = v.tmIf(this)
235
   }
   class TmIsZero(val t: Tm) extends Tm {
      def accept[A](v: TmVisit[A]): A = v.tmIsZero(this)
   }
```

The abstract class Tm represents the datatype of terms, and syntactic constructs of terms are subclasses of Tm. A generic accept method is defined throughout the class hierarchy, which is implemented by invoking the corresponding lowercase *visit method* exposed by TmVisit.

270

Visitor Interface. TmVisit is the *visitor interface* that declares all the visit methods required by accept implementations. Its definition is given below:

```
245 trait TmVisit[A] {
    def tmZero(x: TmZero): A
    def tmSucc(x: TmSucc): A
    def tmPred(x: TmPred): A
    def tmTrue(x: TmTrue): A
250 def tmFalse(x: TmFalse): A
    def tmIf(x: TmIf): A
    def tmIsZero(x: TmIsZero): A
}
```

TmVisit is parameterized by A for abstracting over the return type of visit methods. Each visit method takes an instance of its corresponding class and returns a value of A.

Concrete Visitors. Operations over Tm are *concrete visitors* that implement the visitor interface TmVisit. The numeric value checker is defined like this:

```
class Nv extends TmVisit[Boolean] {
    def tmZero(x: TmZero) = true
    def tmSucc(x: TmSucc)= x.t.accept(this)
    def tmPred(x: TmPred) = false
    def tmTrue(x: TmTrue) = false
    def tmFalse(x: TmFalse) = false
    def tmIf(x: TmIf) = false
    def tmIsZero(x: TmIsZero) = false
}
```

Nv implements TmVisit by instantiating the type parameter A as Boolean and giving an implementation to each visit method. Here, the interesting cases are tmZero and tmSucc. For the former, a true is returned; for the latter, we call _.t.accept(this) for recursively applying Nv to check the inner term. The remaining cases are not numeric values thus return false.

With Nv defined, we can now implement the small-step evaluation visitor:

```
class Eval1 extends TmVisit[Tm] {
     val eval1 = this // Dependency on the visitor itself
     val nv = new Nv // Dependency on another visitor
275
     def tmZero(x: TmZero) = throw NoRuleApplies
     def tmSucc(x: TmSucc) = new TmSucc(x.t.accept(this))
     def tmPred(x: TmPred) = x.t.accept(new TmVisit[Tm] {
       def tmZero(y: TmZero) = y
                                                                 // PredZero
       def tmSucc (y: TmSucc) =
280
         if (y.t.accept(nv)) y.t
                                                                 // PredSucc
         else new TmPred(y.t.accept(eval1))
                                                                 // Pred
                                                                 // Pred
       def tmPred(y: TmPred) = new TmPred(y.accept(eval1))
       def tmTrue(y: TmTrue) = new TmPred(y.accept(eval1))
                                                                 // Pred
       def tmFalse(y: TmFalse) = new TmPred(y.accept(eval1))
                                                                // Pred
285
       def tmIf(y: TmIf) = new TmPred(y.accept(eval1))
                                                                 // Pred
        def tmIsZero(y: TmIsZero) = new TmPred(y.accept(eval1)) // Pred
     })
     def tmTrue(x: TmTrue) = throw NoRuleApplies
     def tmFalse(x: TmFalse) = throw NoRuleApplies
290
     def tmIf(x: TmIf) = x.t1.accept(new TmVisit[Tm] {
```

```
def tmTrue(y: TmTrue) = x.t2
        def tmFalse(y: TmFalse) = x.t3
        def tmZero(y: TmZero) = new TmIf(y.accept(eval1),x.t2,x.t3)
        def tmSucc(y: TmSucc) = new TmIf(y.accept(eval1),x.t2,x.t3)
295
        def tmPred(y: TmPred) = new TmIf(y.accept(eval1),x.t2,x.t3)
        def tmIf(y: TmIf) = new TmIf(y.accept(eval1),x.t2,x.t3)
        def tmIsZero(y: TmIsZero) = new TmIf(y.accept(eval1),x.t2,x.t3)
      })
      def tmIsZero(x: TmIsZero) = x.t.accept(new TmVisit[Tm] {
300
        def tmZero(y: TmZero) = new TmTrue
        def tmSucc (y: TmSucc) =
          if (y.t.accept(nv)) new TmFalse
          else new TmIsZero(y.accept(eval1))
        def tmPred(y: TmPred) = new TmIsZero(y.accept(eval1))
305
        def tmTrue(y: TmTrue) = new TmIsZero(y.accept(eval1))
        def tmFalse(y: TmFalse) = new TmIsZero(y.accept(eval1))
        def tmIf(y: TmIf) = new TmIsZero(y.accept(eval1))
        def tmIsZero(y: TmIsZero) = new TmIsZero(y.accept(eval1))
310
     })
   7
```

The small-step evaluator rewrites a term to another thus A is instantiated as Tm. Since primitive cases are already values, we simply throw a NoRuleApplies exception for tmZero, tmTrue and tmFalse. Defining the case for tmSucc is easy too: we construct a new successor with its inner term rewritten by eval1. In contrast, defining tmPred,

- tmIf and tmIsZero is trickier because they all have multiple rules. Take tmPred for example. As a visitor recognizes only one level representation of a term, it is insufficient to encode rules that require nested case analysis. To further reveal the shape of the inner term, anonymous visitors are created. Rules like PREDSucc can then be specified inside the tmSucc method of the inner visitor. Moreover, the inner visitor of tmPred
- inside the tmSucc method of the inner visitor. Moreover, the inner visitor of tmPred depends on both Eval1 and Nv. These dependencies are expressed by the fields eval1 and nv, which are instantiated as visitor instances. Then we can pass eval1 or nv as an argument to the accept method for using the dependency. Notice that the PRED rule is repeated 6 times. Similar situations also happen in tmIf and tmIsZero, making the overall implementation of Eval1 quite lengthy.

Client Code. We can write some tests for our implementation of ARITH:

```
// iszero (if false then true else pred (succ 0))
val tm = new TmIsZero(
    new TmIf(new TmFalse,new TmTrue,new TmPred(new TmSucc(new TmZero))))
330 val eval1 = new Eval1
val tm1 = tm.accept(eval1) // iszero (pred (succ 0))
val tm2 = tm1.accept(eval1) // iszero 0
val tm3 = tm2.accept(eval1) // 0
where we construct a term using all syntactic forms of the ARITH language and evaluate
335 it step by step using eval1. The evaluation result of each step is shown in the comments
```

335 it step by step using ev on the right hand side.

315

Discussion of the Approach. The conventional VISITOR pattern has been criticized for its *verbosity* and *inextensibility* [28, 29], which are manifested in the implementation of ARITH. Programming with the VISITOR pattern is associated with a lot of infrastructure

code, including the visitor interface, the class hierarchy, etc. Writing such infrastructure manually is tedious and error-prone, especially when there are many classes involved. Such verbosity restricts the usage VISITOR pattern, as Martin [30] wrote:

"Often, something that can be solved with a VISITOR can also be solved by something simpler."

- ³⁴⁵ Moreover, the VISITOR pattern suffers from the Expression Problem [1]: it is *easy* to add new operations by defining new visitors (as illustrated by nv and eval1) but *hard* to add new variants. The reason is that Tm and TmVisit are tightly coupled. When trying to add new subclasses to the Tm hierarchy, it is not possible to implement their accept methods because there exist no corresponding visit methods in TmVisit. A non-
- solution is to modify TmVisit with new visit methods. As a consequence, all existing concrete implementations of TmVisit have to be modified in order to account for those variants. This violates the "*no modification on existing code*" principle of the Expression Problem. Modification is even impossible if the source code is unavailable. As a result, NAT and BOOL cannot be separated from ARITH. Thus, the whole implementation is
 neither extensible nor composable. Nevertheless, the exhaustiveness on visit methods is
- guaranteed since a class cannot contain any abstract methods.
 - 2.4. Sealed Case Classes

The VISITOR pattern is often used as a poor man's approach to pattern matching in OO languages. Fortunately, Scala [31] is a language that unifies functional and OO paradigms and supports pattern matching natively via case classes/extractors [32]. Case classes can be either open or sealed. Sealed case classes are close to algebraic datatypes

in functional languages, which have a fixed set of variants.

Representing the Tm hierarchy using sealed case classes looks like this:

```
sealed trait Tm
```

380

```
case object TmZero extends Tm
case class TmSucc(t: Tm) extends Tm
case class TmPred(t: Tm) extends Tm
case object TmTrue extends Tm
case object TmFalse extends Tm
case class TmIf(t1: Tm, t2: Tm, t3: Tm) extends Tm
```

- case class TmIsZero(t: Tm) extends Tm
 The differences are that Tm is a sealed trait and variants of Tm are additionally marked
 as case. Also, no-argument variants are Scala's singleton objects and fields of case
 classes are by default val.
- The case keyword triggers the Scala compiler to automatically inject methods into a class, including a constructor method (apply) and an extractor method (unapply). The injected constructor method simplifies creating objects from case classes. For example, a successor application to zero can be constructed via TmSucc(TmZero). Conversely, the injected extractor enables tearing down an object via pattern matching.

The numeric value checker can be defined by pattern matching on the term:

```
def nv(t: Tm): Boolean = t match {
    case TmZero => true
    case TmSucc(t1) => nv(t1)
    case _ => false
285 }
```

The term t is matched sequentially against a series of patterns (case clauses). For example, TmSucc(TmZero) will be handled by the second case clause of nv, which recursively invokes nv on its subterm t1 (which is TmZero). Then, TmTrue will be matched by the first case clause with a true returned eventually. A wildcard pattern (_) is used in the last case clause for handling boring cases altogether.

The strength of pattern matching shines in encoding the small-step semantics:

```
def eval1(t: Tm): Tm = t match {
     case TmSucc(t1) => TmSucc(eval1(t1))
     case TmPred(TmZero) => TmZero
                                              // PredZero
395
     case TmPred(TmSucc(t1)) if nv(t1) => t1 // PredSucc
     case TmPred(t1) => TmPred(eval1(t1))
                                              // Pred
     case TmIf(TmTrue,t2,_) => t2
     case TmIf(TmFalse,_,t3) => t3
     case TmIf(t1,t2,t3) => TmIf(eval1(t1),t2,t3)
     case TmIsZero(TmZero) => TmTrue
400
     case TmIsZero(TmSucc(t1)) if nv(t1) => TmFalse
     case TmIsZero(t1) => TmIsZero(eval1(t1))
     case _ => throw NoRuleApplies
   7
```

- With the help of pattern matching, the overall definition is a direct mapping from the 405 formalization shown in Figure 1. There is a one-to-one correspondence between the rules and the case clauses. For example, PREDSUCC is concisely described by a *deep* pattern (TmPred(TmSucc(t1))) with a guard (if nv(t1)) and PRED is captured only once by TmPred(t1).
- *Client Code.* The client code is also more natural and compact than that in visitors: 410

```
val tm = TmIsZero(TmIf(TmFalse,TmTrue,TmPred(TmSucc(TmZero))))
val tm1 = eval1(tm) // iszero (pred (succ 0))
val tm2 = eval1(tm1) // iszero 0
val tm3 = eval1(tm2) // 0
```

Discussion of the Approach. The ARITH implementation using sealed case classes is very concise. Moreover, sealed case classes facilitate exhaustiveness checking on patterns since all variants are statically known. If we forgot to write the wildcard pattern in nv, the Scala compiler would warn us that a case clause for TmPred is missing. An

exception is eval1, whose exhaustiveness is not checked by the compiler due to the use 420 of guards. The reason is that a guard might call some function whose execution result is only known at runtime, making the reachability of that pattern difficult to decide statically. The price to pay for exhaustiveness is the inability to add new variants of Tm in separate files. Thus, like the visitor version, the implementation is neither extensible nor composable. 425

430

390

2.5. Open Case Classes

While the implementation using sealed case classes is concise, it is not modular because ARITH is still defined as a whole. To separate out NAT and BOOL, we turn to open case classes by trading exhaustiveness checking for the ability to add new variants in separate files. To make up for the loss of exhaustiveness, Zenger and Odersky's idea

⁴¹⁵ where **new** clauses are no longer needed.

of *Extensible Algebraic Datatypes with Defaults* (EADDs) [33] can be applied. The key idea is to always use a default in each operation to handle variants that are not explicitly mentioned. The existence of a default makes operations extensible, as variants added later will be automatically subsumed by that default. If the extended variants have behavior different from the default, we can define a new operation that deals with

the extended variants and delegates to the old operation.

435

465

We first remove the sealed constraint on Tm and specify the default behavior of eval1 inside a trait Term:

```
trait Term {
      trait Tm
440
      def eval1(t: Tm): Tm = throw NoRuleApplies
    }
       Then, NAT can be defined as an extended trait for Term:
    trait Nat extends Term {
      case object TmZero extends Tm
445
      case class TmSucc(t: Tm) extends Tm
      case class TmPred(t: Tm) extends Tm
      def nv(t: Tm): Boolean = t match {
        case TmZero => true
        case TmSucc(t1) => nv(t1)
450
        case _ => false
      }
      override def eval1(t: Tm): Tm = t match {
        case TmSucc(t1) => TmSucc(eval1(t1))
        case TmPred(TmZero) => TmZero
                                                  // PredZero
455
        case TmPred(TmSucc(t1)) if nv(t1) => t1 // PredSucc
        case TmPred(t1) => TmPred(eval1(t1))
                                                  // Pred
        case _ => super.eval1(t)
      }
   }
460
```

Nat introduces TmZero, TmSucc and TmPred as variants of Tm. nv is defined in the old way. eval1 is overridden with case clauses for TmSucc and TmPred, and TmZero is dealt by Term's eval1 via a super call.

Similarly, BooL is defined as another trait that extends Tm with its own variants and eval1:

```
trait Bool extends Tm {
    case object TmTrue extends Tm
    case object TmFalse extends Tm
    case class TmIf(t1: Tm,t2: Tm,t3: Tm) extends Tm
    override def eval1(t: Tm): Tm = t match {
        case TmIf(TmTrue,t2,_) => t2
        case TmIf(TmFalse,_,t3) => t3
        case TmIf(t1,t2,t3) => TmIf(eval1(t1),t2,t3)
        case _ => super.eval1(t)
475    }
}
```

Finally, ARITH can be defined as a unification of NAT and BOOL implementations:

```
trait Arith extends Nat with Bool {
    case class TmIsZero(t: Tm) extends Tm
    override def eval1(t: Tm) = t match {
        case TmIsZero(TmZero) => TmTrue
```

```
case TmIsZero(TmSucc(t1)) if nv(t1) => TmFalse
        case TmIsZero(t1) => TmIsZero(eval1(t1))
       case TmZero => super[Nat].eval1(t)
       case _: TmSucc => super[Nat].eval1(t)
485
       case _: TmPred => super[Nat].eval1(t)
        case _ => super[Bool].eval1(t)
     }
   }
```

```
490
```

Scala's mixin composition allows Arith to extend both Nat and Bool. The definition nv inherited from Nat works well in Arith, as it happens to have a very good default that automatically fits for the new cases. For instance, calling nv(TmFalse) returns false as expected. However, overridding eval1 becomes problematic. We cannot simply complement the cases for TmIsZero and handle all the inherited cases at once since both Nat and Bool are extended. Instead we have to separate the inherited cases using typecases and delegate appropriately to either Nat or Bool via super calls.

Discussion of the Approach. Combining open case classes with EADDs brings extensibility. This idea works well for linear extensions (such as NAT and BOOL) but not so well for non-linear extensions like ARITH. As shown by eval1 in Arith, composing non-linear extensions is tedious and error-prone. Without any assistance from the Scala 500 compiler during this process, it is rather easy to make mistakes like forgetting to delegate a case or delegating a case to a wrong parent. Moreover, the exhaustiveness checking on case clauses is lost. Although in the spirit of EADDs case clauses should always end with a wildcard that ensures exhaustiveness, it is not enforced by the Scala compiler.

```
2.6. Partial Functions
```

To ease the composition of Nat and Bool, one may consider Scala's PartialFunction. PartialFunction provides an orElse method for composing partial functions. orElse tries the composed partial functions sequentially until no MatchError is raised.

The open case class version of ARITH can be adapted to a partial function version with a few changes. First, eval1 in Term should be declared as a partial function:

```
def eval1: PartialFunction[Tm.Tm]
```

Second, wildcards cannot be used in implementing eval1 anymore because they will shadow other partial functions to be composed. For example, eval1 in Bool is rewritten as:

```
override def eval1 {
515
     case TmIf(TmTrue,t2,_) => t2
     case TmIf(TmFalse,_,t3) => t3
     case TmIf(t1,t2,t3) => TmIf(eval1(t1),t2,t3)
     case TmTrue => throw NoRuleApplies
     case TmFalse => throw NoRuleApplies
520
   }
```

510

An instance of PartialFunction [Tm, Tm] is constructed using the anonymous function syntax with the argument Tm being directly pattern matched. The wildcard pattern is replaced by two constructor patterns TmTrue and TmFalse with identical right hand side,

525 losing some convenience. Nevertheless, partial functions make the composition work more smoothly, avoiding the problems caused by the open case classes approach:

```
override def eval1 = super[Nat].eval1 orElse super[Bool].eval1 orElse {
     case TmIsZero(TmZero) => TmTrue
     case TmIsZero(TmSucc(t1)) if nv(t1) => TmFalse
     case TmIsZero(t1) => TmIsZero(eval1(t1))
530
   }
```

eval1 is overridden by chaining eval1 from Nat and Bool as well as a new partial function for the zero test using the orElse combinator.

- Discussion of the Approach. Although combining open case classes with partial functions makes the composition smoother, it is still not fully satisfactory. The orElse 535 combinator is left-biased, thus the composition order determines the composed semantics. That is, f orElse g is not equivalent to g orElse f, if f and g are two overlapped partial functions (i.e. containing case clauses with identical left hand side but different right hand side). When composing such overlapped partial functions, orElse gives
- no warning. Also, the semantics of the overlapped patterns are all from either f or g, 540 depending on which comes first. It is not possible to have a mixed semantics for overlapped patterns (e.g. picking case A from f and case B from g when both f and g define case A and case B), which restricts the reusability of partial functions. Lastly, partial functions rely on exception handling, which has a negative impact on performance.

2.7. Extensible Visitors 545

Essentially what makes pattern matching hard to be extended or composed is the order-sensitive semantics of pattern matching and wildcard patterns that cover both known and unknown variants. We think it is useful to distinguish between top-level (shallow) patterns and nested (deep) patterns. Top-level patterns should be orderinsensitive and partitioned into multiple definitions so that they can be easily composed.

We can achieve this by combining open case classes with extensible visitors [34, 10, 35, 21].

The ARITH implementation is organized in a way similar to the open case classes approach. Let us start with Term:

```
trait Term {
555
      type TmV <: TmVisit</pre>
      trait Tm { def accept(v: TmV): v.OTm }
      trait TmVisit { _: TmV =>
        type OTm
        def apply(t: Tm) = t.accept(this)
560
      trait TmDefault extends TmVisit { _: TmV =>
        def tm: Tm => OTm
      }
      trait Eval1 extends TmDefault { _: TmV =>
565
        type OTm = Tm
        def tm = _ => throw NoRuleApplies
      }
      val eval1: Eval1
   }
```

570

550

Instead of using TmVisit in declaring the accept method, we use an abstract type *member* TmV and constrain it to be a *subtype* of TmVisit. This enables invocations on the methods declared inside TmVisit, but at the same time, decouples Tm from TmVisit. The upper bound of the return type of the visit methods is also captured by

an abstract type rather than a type parameter for avoiding reinstantiation in inherited visitors. Accordingly, the return type of accept is now a path dependent type v.OTm. A syntactic sugar method apply is defined inside TmVisit for enabling v(x) as a shorthand of x.accept(v), where x and v are instances of Tm and TmVisit, respectively. To pass this as an argument of accept in implementing apply, we state that TmVisit is of type

TmV using a *self-type annotation*. To mimic wildcards, we use default visitors [36]. But unlike wildcards, default visitors only deal with *known* variants. TmDefault is the default visitor interface, which extends TmVisit with a generic tm method for specifying the default behavior. Eval1 is a default visitor thus it extends TmDefault, specifies the output type OTm as Tm and implements tm. Each concrete visitor has a companion val declaration for allowing themselves to be used in other visitors.

The encoding makes more sense with the implementation of Nat given:

```
trait Nat extends Term {
      type TmV <: TmVisit</pre>
      case object TmZero extends Tm {
        def accept(v: TmV): v.OTm = v.tmZero
590
      3
      case class TmSucc(t: Tm) extends Tm {
        def accept(v: TmV): v.OTm = v.tmSucc(t)
      }
      case class TmPred(t: Tm) extends Tm {
595
        def accept(v: TmV): v.OTm = v.tmPred(t)
      }
      trait TmVisit extends super.TmVisit { _: TmV =>
        def tmZero: OTm
        def tmSucc: TmSucc => OTm
600
        def tmPred: TmPred => OTm
      3
      trait TmDefault extends TmVisit with super.TmDefault { _: TmV =>
        def tmZero = tm(TmZero)
        def tmSucc = tm
605
        def tmPred = tm
      }
      def nv(t: Tm): Boolean = t match {
        case TmZero => true
        case TmSucc(t1) => nv(t1)
610
        case _ => false
      3
      trait Eval1 extends TmDefault with super.Eval1 { _: TmV =>
        override def tmSucc = x => TmSucc(this(x.t))
        override def tmPred = {
615
          case TmPred(TmZero) => TmZero
          case TmPred(TmSucc(t)) if nv(t) => t
          case TmPred(t) => TmPred(this(t))
        }
      }
620
    }
```

Tm is extended with several case classes/objects. Correspondingly TmVisit is extended with new visit methods and TmV is *covariantly refined* as the subtype of the extended TmVisit. Visit methods are declared using Scala's functions instead of ordinary methods

- ⁶²⁵ for two reasons. First, the argument type (e.g. TmSucc) has already been revealed by the method name (tmSucc) and can be inferred by the Scala compiler without losing information. Second, first-class functions facilitate pattern matching on the argument. These two advantages result in a concise definition of Eval1, where the type of x is omitted and a value of TmPred => Tm is constructed by pattern matching.
- ⁶³⁰ Unlike conventional visitors, nested case analysis is much simplified via (nested) pattern matching rather than auxiliary visitors. For example, when a predecessor term is processed by Eval1, it will be recognized and dispatched to the tmPred method. Then the TmPred object is matched by the case clauses. As these are case clauses, deep patterns and guards can be used. To restore the convenience of wildcards for top-level
- patterns, TmDefault is used, which implements visit methods by delegating to tm. Notice that Eval1 is defined as a trait instead of a class for enabling mixin composition. By extending both TmDefault and super.Eval1, Eval1 only needs to override interesting cases.

The numeric value checker is defined as a method rather than a visitor. This is because, as we have discussed, nv is a good candidate for applying EADDs. Of course, nv can be defined as a default visitor like Eval1. But whenever Nat is extended with new terms, the definition of nv has to be refined by composing Nv with the extended TmDefault.

BOOL is defined in a similar manner:

```
trait Bool extends Term {
645
      type TmV <: TmVisit</pre>
      trait TmVisit extends super.TmVisit { _: TmV =>
        def tmTrue: OTm
        def tmFalse: OTm
        def tmIf: TmIf => OTm
650
      }
      trait TmDefault extends TmVisit with super.TmDefault { _: TmV =>
        def tmTrue = tm(TmTrue)
        def tmFalse = tm(TmFalse)
655
        def tmIf = tm
      }
      case object TmTrue extends Tm {
        override def accept(v: TmV) = v.tmTrue
      3
      case object TmFalse extends Tm {
660
        override def accept(v: TmV) = v.tmFalse
      3
      case class TmIf(t1: Tm, t2: Tm, t3: Tm) extends Tm {
        override def accept(v: TmV) = v.tmIf(this)
      3
665
      trait Eval1 extends TmDefault with super.Eval1 { _: TmV =>
        override def tmIf = {
          case TmIf(TmTrue,t2,_) => t2
          case TmIf(TmFalse,_,t3) => t3
          case TmIf(t1,t2,t3) => TmIf(this(t1), t2, t3)
670
        }
     }
   }
```

With case clauses partitioned into visit methods according to their top-level pattern,

```
unifying Nat and Bool becomes easy via Scala's mixin composition:
675
    trait Arith extends Nat with Bool {
      type TmV <: TmVisit</pre>
      case class TmIsZero(t: Tm) extends Tm {
        override def accept(v: TmV) = v.tmIsZero(this)
      }
680
      trait TmVisit extends super[Nat].TmVisit
                    with super[Bool].TmVisit { _: TmV =>
        def tmIsZero: TmIsZero => OTm
      }
685
      trait TmDefault extends TmVisit with super[Nat].TmDefault
                      with super[Bool].TmDefault { _: TmV =>
        def tmIsZero = tm
      }
      trait Eval1 extends TmVisit with super[Nat].Eval1
                  with super[Bool].Eval1 { _: TmV =>
690
        def tmIsZero = {
          case TmIsZero(TmZero) => TmTrue
          case TmIsZero(TmSucc(t)) if nv(t) => TmFalse
          case TmIsZero(t) => TmIsZero(this(t))
       }
695
      }
   }
```

Defining Eval1 for Arith only needs to inherit Eval1 definitions from Nat and Bool and complement the tmIsZero method. Since tmIsZero is an interesting case, Eval1 extends TmVisit rather than TmDefault.

Instantiation. Components defined in this way cannot be directly used in client code. An additional step to instantiate traits into objects is required. Instantiating Arith, for example, is done like this:

```
object Arith extends Arith {
   type TmV = TmVisit
   object eval1 extends Eval1
}
```

700

720

The companion object Arith binds the abstract type TmV to its corresponding the visitor interface TmVisit. The eval1 declaration is met by a singleton object that extends Eval1.

⁷¹⁰ If Eval1 does not implement all the visit methods, the object creation fails, with the missing methods reported.

Client Code. Now we can use the companion object Arith in client code: import Arith._

```
val tm = TmIsZero(TmIf(TmFalse,TmTrue,TmPred(TmSucc(TmZero))))
val tm1 = eval1(tm) // iszero (pred (succ 0))
val tm2 = eval1(tm1) // iszero 0
val tm3 = eval1(tm2) // 0
By importing Arith, the constructors and visitors defined inside Arith are in scope.
```

With the syntactic sugar defined for visitors, a term can be constructed and evaluated identically to the case class version.

Discussion of the Approach. With the powerful extensible visitor encoding, the ARITH implementation is made both extensible and composable. However, extensible visitors

are even more verbose than conventional ones. The use of traits in implementing visitors brings composability but, at the same time, requires extra instantiation code. Another

⁷²⁵ downside of using traits is that the exhaustiveness checking on visit methods is deferred to the instantiation stage. Moreover, the encoding relies on advanced features of Scala, making it less accessible to novice Scala programmers.

2.8. EVF

Programming with visitors can be greatly simplified with the associated infrastructure automatically generated. This idea has been adopted in our previous work on EVF [21], which employs Java annotation processors for generating extensible visitor infrastructure.

EVF employs Object Algebra interfaces [9] to describe the abstract syntax:

```
@Visitor interface TmAlg<Tm> {
   Tm TmZero();
   Tm TmSucc(Tm t);
   Tm TmPred(Tm t);
```

}

735

740

where the type parameter Tm represents the datatype and capitalized methods that return Tm represent variants of Tm. Annotated as @Visitor, TmAlg will be recognized and processed by EVF. Then the infrastructure for TmAlg will be generated, including a class hierarchy, a visitor interface and various default visitors. Based on the generated visitor infrastructure, we are able to implement Nv:

```
interface Nv<Tm> extends TmAlgDefault<Tm,Boolean> {
    @Override default Zero<Boolean> m() {
        return () -> false;
        }
        default Boolean TmZero() {
        return true;
    }
    default Boolean TmSucc(Tm t) {
        return visitTm(t);
     }
    }
}
```

```
<sup>755</sup> Nv is defined as an interface with visit methods implemented using default methods
for retaining composability. The Java extensible visitor encoding adopted by EVF is,
however, not as powerful as the Scala one shown in Section 2.7, which does not support
modular ASTs. Whenever an annotated Object Algebra interface gets extended, a new
class hierarchy is generated. Thus, we cannot refer to a concrete datatype directly in
```

- visitors since this will make them inextensible. Instead, datatypes are kept abstract in visitors. To traverse an abstract datatype like Tm, visitTm is called. visitTm is a method exposed by the generated visitor interface, similar to apply shown in Section 2.7. TmAlgDefault is the default visitor similar to TmDefault, where the default behavior is specified inside m().
- 765 Defining Eval1 is tricker:

```
interface Eval1<Tm> extends TmAlgDefault<Tm,Tm>, tm.Eval1<Tm> {
  TmAlgMatcher<Tm,Tm> matcher(); // Dependency for nested case analysis
  TmAlg<Tm> f(); // Dependency for AST reconstruction
  Nv<Tm> nv(); // Dependency for another visitor
```

There are three dependencies declared using abstract methods. Firstly, since Java does not support native pattern matching, the matcher dependency is convenient for constructing anonymous visitors. matcher returns an instance of the generated TmAlgMatcher interface, which provides fluent setters for defining visit methods via Java 8's lambdas.

⁷⁸⁵ The otherwise setter mimics the wildcard pattern. Secondly, the reconstruction of a term is done via an abstract factory f of type TmAlg<Tm>. Lastly, the abstract method nv expresses the dependency on the visitor Nv.

BOOL is implemented similarly in another package bool, whose definition is omitted. The implementation of ARITH is more interesting, which is shown below:

```
@Visitor interface TmAlg<Tm> extends nat.TmAlg<Tm>, bool.TmAlg<Tm> {
790
     Tm TmIsZero(Tm t);
   }
   interface Eval1<Tm> extends GTmAlg<Tm,Tm>,bool.Eval1<Tm>,nat.Eval1<Tm> {
     TmAlgMatcher<Tm,Tm> matcher(); // Dependency refinement
     TmAlg<Tm> f();
                                      // Dependency refinement
795
     default Tm TmIsZero(Tm t) {
       return matcher()
          .TmZero(() -> f().TmTrue())
          .TmSucc(t1 -> nv(t1) ? f().TmFalse() : f().TmIsZero(visitTm(t)))
          .otherwise(() -> f().TmIsZero(visitTm(t)))
800
          .visitTm(t);
     }
   7
   interface Nv<Tm> extends TmAlgDefault<Tm,Boolean>, nat.Nv<Tm> {}
```

NAT and BOOL implementations are merged using Java 8' multiple interface inheritance. Despite complementing TmIsZero, return types of dependencies are covariantly refined for allowing TmIsZero calls. Since Nv is implemented as a visitor, it needs to be refined as well.

Instantiation. Instantiating interfaces into classes for creating objects is also required:

```
810 static class NvImpl implements Nv<CTm>, TmAlgVisitor<Boolean> {}
static class Eval1Impl implements Eval1<CTm>, TmAlgVisitor<CTm> {
    public TmAlg<CTm> f() { return f; }
    public TmAlgMatcher<CTm,CTm> matcher() {
        return new TmAlgMatcherImpl<>();
815 }
    public Nv<CTm> nv() { return nv; }
    }
    static TmAlgFactory f = new TmAlgFactory();
    static NvImpl nv = new NvImpl();
820 static Eval1Impl eval1 = new Eval1Impl();
```

The interfaces are instantiated into classes with a suffix Impl. Eval1Impl, for example, implements Eval1 by: 1) instantiating Tm as the generated datatype CTm; 2) inheriting the generated TmAlgVisitor for a visitTm implementation; 3) fullfilling the dependencies using TmAlgFactory, TmAlgMatcherImpl and NvImpl respectively.

Client Code. The term is constructed via the factory object f and can be evaluated like this:

```
CTm tm = f.TmIsZero(
   f.TmIf(f.TmFalse(),f.TmTrue(),f.TmPred(f.TmSucc(f.TmZero()))));
eval1.visitTm(eval1.visitTm(eval1.visitTm(tm)))
```

- Discussion of the Approach. EVF simplifies programming with visitors through code generation. It further addresses the extensibility issue by adopting extensible visitors. Restricted by Java, nested case analysis in EVF is done by means of anonymous visitors, which is not as expressive and concise as pattern matching in Scala. To enable composability, EVF visitors are defined using Java 8's interfaces with default methods—
- in the same spirit of using traits in Scala. Consequently, the exhaustiveness checking on the top-level visit methods is lost in visitor definition site and is delayed to the visitor instantiation site. Nevertheless, the exhaustiveness on the visit methods of the anonymous visitors is guaranteed because the otherwise setter must be called when constructing an anonymous visitor.
- 840 2.9. CASTOR

Highly inspired by EVF, CASTOR is a Scala framework designed for programming with generative, extensible visitors. CASTOR improves on EVF in two aspects. First, CASTOR adopts a more powerful Scala extensible visitor encoding presented in Section 2.7 that additionally enables pattern matching, GADTs, hierarchical datatypes, graphs, etc.

Second, CASTOR employs Scalameta for annotation processing, which allows not only generating new code based on the annotated code but also modifying the annotated code itself. These extra abilities together result in more concise and expressive visitor code than that in EVF. We next give a modular implementation of ARITH using CASTOR, which has a one-to-one correspondence with the code shown in Section 2.7.

Let us start with the root component Term:

```
@family trait Term {
    @adt trait Tm
    @default(Tm) trait Eval1 {
        type OTm = Tm
    &ss def tm = _ => throw NoRuleApplies
    }
}
```

Several CASTOR'S annotations are employed: @family denotes a CASTOR'S component; @adt denotes a datatype; @default(Tm) denotes a default visitor on Tm. Compared to the

Term definition shown in Section 2.7, the definition here is much simplified. The accept declaration, the type member TmV, the visitor interface TmVisit and the default visitor TmDefault are all generated by analyzing the @adt definition of Tm. Similarly, CASTOR adds the extends clause, the self type annotation and the corresponding val declaration for Eval1 by the annotation @default(Tm).

⁸⁶⁵ Defining Nat is also much simplified:

```
@family trait Nat extends Term {
      @adt trait Tm extends super.Tm {
        case object TmZero
        case class TmSucc(t: Tm)
        case class TmPred(t: Tm)
870
      3
      def nv(t: Tm): Boolean = t match {
        case TmZero => true
        case TmSucc(t1) \Rightarrow nv(t1)
        case _ => false
875
      }
      @default(Tm) trait Eval1 extends super.Eval1 {
        override def tmSucc = x => TmSucc(this(x.t))
        override def tmPred = {
          case TmPred(TmZero) => TmZero
880
          case TmPred(TmSucc(t)) if nv(t) => t
          case TmPred(t) => TmPred(this(t))
        7
      }
   }
885
```

Variants of Tm are declared inside Tm. CASTOR will pull them outside of Tm and automatically complement the extends clause and the accept method definition. Since new variants of Tm are introduced, CASTOR will add the extended TmVisit, TmDefault and refined TmV to Nat.

⁸⁹⁰ Similarly, Bool can be defined as follows:

```
@family trait Bool extends Term {
      @adt trait Tm extends super.Tm {
        case object TmTrue
        case object TmFalse
        case class TmIf(t1: Tm, t2: Tm, t3: Tm)
895
      }
      @default(Tm) trait Eval1 extends super.Eval1 {
        override def tmIf = {
          case TmIf(TmTrue,t2,_) => t2
          case TmIf(TmFalse,_,t3) => t3
900
          case TmIf(t1,t2,t3) => TmIf(this(t1),t2,t3)
        }
      }
   }
       The code below finishes the ARITH implementation:
905
   @family trait Arith extends Nat with Bool {
      @adt trait Tm extends super[Nat].Tm with super[Bool].Tm {
        case class TmIsZero(t: Tm)
      }
      @visit(Tm) trait Eval1 extends super[Nat].Eval1
910
                              with super[Bool].Eval1 {
        def tmIsZero = {
          case TmIsZero(TmZero) => TmTrue
          case TmIsZero(TmSucc(t)) if nv(t) => TmFalse
          case TmIsZero(t) => TmIsZero(this(t))
915
       }
     }
   }
```

Since the TmIsZero is an interesting case for Eval1, @visit annotation is used, which denotes an ordinary visitor. Thus, Eval1 extends TmVisit after transformation.

Client Code. A @family trait can be directly imported in client code since CASTOR automatically generates a companion object for it: import Arith.

val tm = TmIsZero(TmIf(TmFalse,TmTrue,TmPred(TmSucc(TmZero))))
val tm1 = eval1(tm) // iszero (pred (succ 0))
val tm2 = eval1(tm1) // iszero 0
val tm3 = eval1(tm2) // 0

which is identical to the client code for Scala extensible visitors shown in Section 2.7.

Discussion of the Approach. We discuss how CASTOR addresses the four properties:

- **Conciseness.** By employing Scala's concise syntax and metaprogramming, CAs-TOR greatly simplifies the definition and usage of visitors. In particular, the need for auxiliary visitors in performing deep case analysis is now replaced by pattern matching via case clauses. The concept of visitors is even made transparent to the end-user, making the framework more user-friendly.
- Exhaustiveness. The exhaustiveness of patterns in CASTOR consists of two parts. The exhaustiveness of visit methods is checked by the Scala compiler when generating companion objects. For nested patterns using case clauses, a default must be provided. However, this default is neither statically enforced by Scala nor CASTOR. Note, however, that with specialized language support it is possible to enforce that nested patterns always provide a default. This is precisely what EADDs [33] do.
 - Extensibility. As illustrated by Nat, Bool and Arith, we can extend the datatype with new variants and operations, modularly. Such extensibility is enabled by the underlying extensible visitor encoding.
- **Composability.** CASTOR obtains composability via Scala's mixin composition, as illustrated by Arith. Unlike partial functions, which silently compose overlapped patterns, composing overlapped patterns in CASTOR will trigger compilation errors because they are conflicting methods from different traits. The error message will indicate the source of conflicts and we are free to select an implementation in resolving the conflict. The composition order does not matter as well.

Table 1 summarizes the evaluation on pattern matching approaches abovementioned in terms of conciseness, exhaustiveness, extensibility, and composability. CASTOR is compared favorably in terms of the four properties among the approaches.

3. Hierarchical Datatypes

⁹⁵⁵ Traditional functional style datatypes are *flat*: variants have no relationships among each other. In contrast, object-oriented style datatypes (i.e. data structures modeled as class hierarchies) can be *hierarchical*: a variant can extend intermediate datatypes

Table 1: Pattern matching support comparison: \bullet = good, \bullet = neutral, \bigcirc = bad.						
	Conciseness	Exhaustiveness	Extensibility	Composability		
Conventional visitors	0	•	0	0		
Sealed case classes	•	•	0	0		
Open case classes	•	0	•	0		
Partial functions	•	0	•	lacksquare		
Extensible visitors	0	0	•	•		
EVF	lacksquare	lacksquare	•	•		
Castor	•	\bullet^*	•	•		

* CASTOR only gets half score on exhaustiveness because *for nested case analysis Scala cannot enforce a default*. In a language-based approach nested case analysis should always require a default, thus fully supporting exhaustiveness.

and/or an existing variant. In other words, while OO style class hierarchies can be arbitrarily deep, typical functional datatypes would correspond to a hierarchy where the depth is always one.

Hierarchical datatypes facilitate reuse. The subtyping relation allows the semantics defined for supertypes to be reused in subtypes. CASTOR supports both styles of datatypes. In this section, we illustrate CASTOR's support for hierarchical datatypes by revising the ARITH language. Another form of hierarchical datatypes will be shown in Section 5,

965 where a new variant is introduced by refining an existing variant. Moreover, the case study on UML Activity Diagrams Section 8 further illustrates the application of hierarchical datatypes.

3.1. Flat Datatypes versus Hierarchical Datatypes

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Terms of the ARITH language shown in Section 2 are represented as a flat datatype, where all the variants extend the root datatype Tm. In fact, terms can be organized in a hierarchical manner according to their types and arities. Figure 2 visualizes the hierarchical representation of terms and the following code materializes it using CASTOR:

```
@adt trait Tm {
     trait TmNullary
     trait TmUnary { val t: Tm }
975
     trait TmTernary { val t1, t2, t3: Tm }
     trait TmNat extends TmNullary
     trait TmBool extends TmNullary
     trait TmNat2Nat extends TmUnary
     trait TmNat2Bool extends TmUnary
980
     case object TmZero extends TmNat
     case class TmSucc(t: Tm) extends TmNat2Nat
     case class TmPred(t: Tm) extends TmNat2Nat
     case object TmTrue extends TmBool
     case object TmFalse extends TmBool
985
     case class TmIf(t1: Tm, t2: Tm, t3: Tm) extends TmTernary
     case class TmIsZero(t: Tm) extends TmNat2Bool
   }
```

The hierarchy becomes multi-layered, where several intermediate datatypes are introduced and case classes/objects do not directly extend the root but an intermediate datatype. Traits in the second layer (TmNullary, TmUnary and TmTernary) classify terms



Figure 2: Hierarchical representation of ARITH terms.

according to their arities. Based on arities, traits in the third layer (TmNat, TmBool, TmNat2Nat, TmNat2Bool) further classify terms according to their types. Concrete case classes/objects are in the fourth layer that extend a corresponding intermediate datatypes. For example, both TmSucc and TmPred extend TmNat2Nat.

3.2. Explicit Delegations

Now we illustrate the advantages of hierarchical datatypes. Suppose we would like to define a printer for ARITH that prints out a term using an S-expression like format. For example, TmIsZero(TmIf(TmFalse,TmTrue,TmPred(TmSucc(TmZero)))) is printed as "(iszero (if false true (pred (succ 0))))". With terms being classified according to their arities, the printer can be modularized:

```
@visit(Tm) trait Print {
    type 0Tm = String
    def tmUnary(x: TmUnary, op: String) = "(" + op + " " + this(x.t) + ")"
    def tmSucc = tmUnary(_,"succ")
    def tmPred = tmUnary(_,"pred")
    def tmIsZero = tmUnary(_,"iszero")
    def tmZero = "0"
    def tmTrue = "true"
    def tmFalse = "false"
    def tmIf = x =>
        "(if " + this(x.t1) + " " + this(x.t2) + " " + this(x.t3) + ")"
}
```

Since all unary terms (TmSucc, TmPred and TmIsZero) are printed in the same way except for the operator, we define an auxiliary method tmUnary. Taking a TmUnary instance and an operator string as arguments, tmUnary puts the parentheses around the operator and the printed inner term of TmUnary. Then, tmSucc, tmPred and tmIsZero are implemented just by calling tmUnary with their respective instance and operator string.

3.3. Default Visitors

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The previous example has shown how to enhance the modularity through explicit delegations. When subtypes share the same behavior with supertypes, the explicit delegations can be eliminated with the help of the generated default visitor. Currently, the ARITH language presented allows ill-typed terms such as TmPred(TmTrue) to be constructed. To rule out these ill-typed terms, typechecking is needed. Some of the

terms share typing rules: TmTrue and TmFalse; TmSucc and TmPred. With CASTOR's default visitor, we can avoid duplication of typing rules:

```
@adt trait Ty {
      case object TyNat
      case object TyBool
   }
1030
    @default(Tm) trait Typeof {
      type OTm = Option[Ty]
      override def tmBool = _ => Some(TyBool)
      override def tmNat = _ => Some(TyNat)
      override def tmNat2Nat = x => this(x.t) match {
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        case Some(TyNat) => Some(TyNat)
        case _ => None
      }
      override def tmNat2Bool = x => this(x.t) match {
        case Some(TyNat) => Some(TyBool)
1040
        case _ => None
      3
      override def tmIf = x => (this(x.t1),this(x.t2),this(x.t3)) match {
        case (Some(TyBool),ty1,ty2) if ty1 == ty2 => this(x.t2)
        case _ => None
1045
      }
      def tm = _ => None
    }
```

Like Tm, Ty is a datatype for representing types, where TyNat and TyBool are two concrete types. A visitor Typeof is defined for typechecking terms. The output type of Typeof is Option[Ty], indicating that if a term is well-typed, some type will be returned; otherwise a None will be returned. Except for TmIf, typing rules are defined on intermediate datatypes. For example, tmNat2Nat is overridden, which checks whether its inner term is of type TyNat and returns TyNat if so. tmSucc and tmPred are implicitly implemented by the inherited default visitor, whose definition is given below:

```
trait TmDefault extends TmVisit { _: TmV =>
      def tm: Tm => OTm
      def tmNullary = (x: TmNullary) => tm(x)
      def tmUnary = (x: TmUnary) => tm(x)
1060
      def tmTernary = (x: TmTernary) => tm(x)
      def tmNat = (x: TmNat) => tmNullary(x)
      def tmBool = (x: TmBool) => tmNullary(x)
      def tmNat2Nat = (x: TmNat2Nat) => tmUnary(x)
      def tmNat2Bool = (x: TmNat2Bool) => tmUnary(x)
      def tmZero = tmNat(TmZero)
1065
      def tmSucc = tmNat2Nat(_)
      def tmPred = tmNat2Nat(_)
      def tmTrue = tmBool(TmTrue)
      def tmFalse = tmBool(TmFalse)
      def tmIf = tmTernary(_)
1070
      def tmIsZero = tmNat2Bool(_)
    }
```

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We can see that the default visitor extends the visitor interface with visit methods for intermediate datatypes and each visit method is implemented by delegating to its direct parent's visit method.

4. GADTs and Well-Typed EDSLs

In this section, we show the support for generalized algebraic data types (GADTs) [37] in CASTOR. GADTs allow not only datatypes to be parameterized but also wellformedness constraints to be expressed in constructors. GADTs are widely used for building well-typed domain-specific languages (EDSLs), which exploit the type system 1080 of the host language to typecheck the terms of the EDSL. Popular approaches to EDSLs like Finally Tagless [11] can provide an encoding of GADTs and provide modularity as well. However, the encoding employed by Finally Tagless is based on Church encodings. Unfortunately, this makes it hard to model several operations that require nested patterns or operations with dependencies. The interested reader is referred to Section 2 and 3 of the EVF paper [21] for a detailed discussion on the issue of Church encodings. We show that just as Finally Tagless encodings, modularity is supported; and like GADTs nested pattern matching and dependencies are easy to do as well.

4.1. GADTs and Well-Typed Terms

We have shown how to rule out ill-typed terms using a type-checking algorithm in 1090 Section 3.3. A better solution, however, is to prevent such terms from being constructed in the first place. This is possible through representing ARITH terms using a GADT-style:

```
@family trait GArith {
      @adt trait Tm[A] {
        case object TmZero extends Tm[Int]
1095
        case class TmSucc(t: Tm[Int]) extends Tm[Int]
        case class TmPred(t: Tm[Int]) extends Tm[Int]
        case object TmTrue extends Tm[Boolean]
        case object TmFalse extends Tm[Boolean]
        case class TmIf[A](t1: Tm[Boolean], t2: Tm[A], t3: Tm[A])
1100
          extends Tm[A]
        case class TmIsZero(t: Tm[Int]) extends Tm[Boolean]
      }
    }
```

- Tm is now parameterized by a type parameter A. When declaring variants of Tm, the 1105 extends clause cannot be omitted anymore since CASTOR does not know how to instantiate A. Notice that A is instantiated differently as Int or Boolean for expressing well-formedness constraints. For example, TmIsZero requires its subterm t of type Tm[Int]. Consequently, one cannot supply a term of type Tm[Boolean] constructed from TmTrue, TmFalse or TmIsZero to TmIsZero. Therefore, ill-formed terms are stati-
- 1110 cally rejected by the Scala type system:

TmIsZero(TmZero) // Accepted! TmIsZero(TmTrue) // Rejected!

4.2. Well-Typed Big-Step Evaluator

As opposed to small-step semantics, big-step semantics immediately evaluates a 1115 valid term to a value. In the case of ARITH, a term can either be evaluated to an integer or a boolean value. Without GADTs, implementing a big-step evaluator for ARITH is tedious:

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```
@family @adts(Tm) @ops(Eval1) trait EvalArith extends Arith {
      @adt trait Value {
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        case class IntValue(v: Int)
        case class BoolValue(v: Boolean)
      }
      @visit(Tm) trait Eval {
1125
         type OTm = Value
        def tmZero = IntValue(0)
        def tmSucc = x => this(x.t) match {
           case IntValue(n) => IntValue(n+1)
           case _ => throw NoRuleApplies
        }
1130
        def tmPred = x => this(x.t) match {
           case IntValue(n) => IntValue(n-1)
           case _ => throw NoRuleApplies
        }
        def tmTrue = BoolValue(true)
1135
        def tmFalse = BoolValue(false)
        def tmIf = x => this(x.t1) match {
           case BoolValue(true) => this(x.t2)
           case BoolValue(false) => this(x.t3)
           case _ => throw NoRuleApplies
1140
        }
        def tmIsZero = x => this(x.t) match {
           case IntValue(0) => BoolValue(true)
           case IntValue(_) => BoolValue(false)
           case _ => throw NoRuleApplies
1145
        }
      }
    }
```

EvalArith illustrates the operation extensibility of CASTOR, which does not introduce any
new variants of Tm but a new visitor Eval on Tm. Auxiliary annotations @adts and @ops
provide inherited datatypes and operations for CASTOR to generate the companion object.
Such an implementation suffers from the so-called *tag* problem [11]: to accommodate different evaluation result types, an open datatype Value is defined for accommodating integers, booleans and many other evaluation result types that might be added in the
future. The two variants IntValue and BoolValue are introduced for wrapping integers and boolean values, respectively. Pattern matching is used for unwrapping the evaluation results from inner terms. A defensive wildcard is needed for dealing with ill-typed terms. We can see that the tagging overhead is high.

Fortunately, we can avoid the tag problem with the help of CASTOR'S GADTs. The extensible visitor encoding for GADTs is slightly different from the one presented in Section 2.7, which additionally take the type information carried by terms into account. For instance, the visitor interface generated for Tm[A] is listed below:

```
trait TmVisit { _: TmV =>
    type OTm[A]

1165  def apply[A](x: Tm[A]) = x.accept(this)
    def tmZero: OTm[Int]
    def tmSucc: TmSucc => OTm[Int]
    def tmPred: TmPred => OTm[Int]
    def tmTrue: OTm[Boolean]
1170  def tmFalse: OTm[Boolean]
```

```
def tmIf[A]: TmIf[A] => OTm[A]
  def tmIsZero: TmIsZero => OTm[Boolean]
}
```

Each visit method now returns a value of a higher-kinded type OTm[A], where A is instantiated consistently with how it is instantiated in the extends clause. For example, tmZero is of type OTm[Int] while tmTrue is of type OTm[Boolean]. Then, a well-typed big-step evaluator can be made *tagless*:

```
@family @adts(Tm) trait EvalGArith extends GArith {
    @visit(Tm) trait Eval {
        type OTm[A] = A
        def tmZero = 0
        def tmSucc = x => this(x.t) + 1
        def tmPred = x => this(x.t) - 1
        def tmTrue = true
        test the def tmFalse = false
        def tmIsZero = x => if (this(x.t1)) this(x.t2) else this(x.t3)
        def tmIsZero = x => this(x.t) == 0
    }
}
```

¹¹⁹⁰ With the output type specified as A, the visit method returns a value of the type carried by the term. For example, visit methods tmZero and tmTrue return Int and Boolean values respectively. Moreover, this Eval implementation remains retroactive when terms of new types (such as Tm[Float]) are introduced.

Here are some terms that have different evaluation result types.

```
import EvalGArith._
eval(TmSucc(TmZero)) // 1
eval(TmIsZero(TmZero)) // true
```

4.3. Well-Typed Small-Step Evaluator

Well-typed big-step evaluators can be defined with Finally Tagless in an equally simple manner. What distinguishes CASTOR from Finally Tagless is the ability to define small-step evaluators in an easy way. The need for deep patterns and the dependency on a numeric value checker causes immediate trouble for Finally Tagless. Although workarounds may be possible for some of the issues, they are cumbersome and require significant amounts of boilerplate code [23]. In contrast, encoding small-step semantics in a GADT-style with CASTOR is unproblematic:

```
@family @adts(Tm) trait Eval1Arith extends GArith {
      def nv[A](t: Tm[A]): Boolean = t match {
        case TmZero => true
        case TmSucc(t1) => nv(t1)
1210
        case _ => false
      ľ
      @default(Tm) trait Eval1 {
        type OTm[A] = Tm[A]
        def tm[A] = x => throw NoRuleApplies
1215
        override def tmIf[A] = {
          case TmIf(TmTrue,t2,_) => t2
          case TmIf(TmFalse,_,t3) => t3
          case TmIf(t1,t2,t3) => TmIf(this(t1),t2,t3)
        }
```

```
1220 override def tmIsZero = {
        case TmIsZero(TmZero) => TmTrue
        case TmIsZero(TmSucc(t)) if nv(t) => TmFalse
        case TmIsZero(t) => TmIsZero(this(t))
      }
1225 ... // Other cases are the same as before
    }
}
```

The instantiation of the output type guarantees that the small-step evaluator is *type*preserving. That is, the type carried by a term remains the same after one step of evaluation. For example, calling eval1 on TmZero will never return TmTrue no matter how Eval1 is implemented. The actual definition of Eval1 is almost the same as before except that nv, tm and tmIf become generic. Still, the ability to do nested pattern matching and to call nv in Eval1 is preserved.

4.4. Extension: Higher-Order Abstract Syntax for Name Binding

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A recurring problem in designing EDSLs is how to deal with binders. For example, in lambda calculus, operations involved with names like α -equivalence and capture-avoiding substitution are non-trivial to define. Higher-order abstract syntax (HOAS) [38] avoids these problems through reusing the binding mechanisms provided by the host language. The following code shows how to extend ARITH with simply-typed lambda calculus modularly:

```
@family trait HOAS extends EvalGArith {
    @adt trait Tm[A] extends super.Tm[A] {
        case class TmVar[A](v: A) extends Tm[A]
        case class TmAbs[A,B](f: Tm[A] => Tm[B]) extends Tm[A => B]
        case class TmApp[A,B](t1: Tm[A => B], t2: Tm[A]) extends Tm[B]
    }
    @visit(Tm) trait Eval extends super.Eval {
        def tmVar[A] = _.v
        def tmAbs[A,B] = x => y => this(x.f(TmVar(y)))
        def tmApp[A,B] = x => this(x.t1)(this(x.t2))
    }
}
```

Three new forms of terms are introduced: lifters (TmVar), lambda abstractions (TmAbs) and applications (TmApp). Of particular interest is TmAbs, which constructs a term of type Tm[A => B] from a Scala lambda function Tm[A] => Tm[B] and thus is *higher-order*.

Correspondingly, Eval is extended with three new visit method implementations. tmVar simply extracts the value out of the lifter. tmAbs is trickier since it returns a value of type A => B. A lambda function is hence created, which takes y of type A and lifts it into Tm[A] using TmVar, then applies x.f to the lifted term for computing a Tm[B] and finally does a recursive call to evaluate Tm[B] into B. tmApp recursively evaluates t1 and t2, which returns the value A => B and A respectively. Then it applies A => B to A for getting a value of B.

Here is an example that illustrates the use of HOAS:

import HOAS._

1265 eval(TmApp(TmAbs((t: Tm[Int]) => TmSucc(TmSucc(t))), TmZero)) // 2

We first create an abstraction term that applies successor twice to the argument t and then apply it to constant zero. Note that the type of t is explicitly specified because



Figure 3: Class diagram of FSM.

Figure 4: A state machine for controlling a door.

Scala's type system is not powerful enough to infer the type of TmAbs without the type annotation.

1270 5. Graphs and Imperative Visitors

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Examples presented so far are all *functional* visitors (i.e. computation is done via returning values) on immutable trees. In fact, CASTOR also supports *imperative* visitors (i.e. computation is done via side effects) and data structures can be mutable graphs. Imperative computation is, in some cases, more efficient than the functional counterpart regarding time and memory. Compared to trees, graphs are a more general data structure that have many important applications. For instance, in the domain of compilers, abstract semantic graphs can be used for representing shared subexpressions, facilitating optimizations like common subexpression elimination. In this section, we show how to model graphs and imperative visitors with CASTOR.

1280 5.1. The Difficulties in Modeling Graphs

Modeling graphs modularly is non-trivial in approaches such as Object Algebras [9]. Consider modeling a Finite State Machine (FSM) language. Figure 3 shows a UML class diagram for the FSM language. A Machine consists of some States. Each State has a name and a number of Transitions. A Transition is triggered by an event, taking one State to another. Concretely, Figure 4 shows a simple state machine for controlling a door, which has three states (opened, closed and locked) and four transitions (close, open, lock and unlock). From Figure 4 we can see that this state machine forms a *graph*, where we can go back and forth from one state to another along with the transitions.

A Failed Attempt with Object Algebras. Let us try to model the FSM language with Object Algebras. Describing the FSM language using a multi-sorted Object Algebra interface is unproblematic:

```
trait FSM[M,S,T] {
    def machine(states: List[S]): M
    def state(name: String, trans: List[T]): S
    def trans(event: String, target: S): T
}
```

where type parameters M, S, T represent different datatypes and factory methods capture their variants. However, constructing a graph using this representation is hard because

Object Algebras support only immutable tree structures that are built *bottom up*. Here is a failed attempt on modeling the door state machine:

```
// Forward reference error!
def door[M,S,T](f: FSM[M,S,T]) = {
    val close: T = f.trans("close",closed)
    val open: T = f.trans("close",closed)
    val lock: T = f.trans("lock",locked)
    val unlock: T = f.trans("unlock",closed)
    val opened: S = f.state("opened", List(close))
    val closed: S = f.state("opened", List(open,lock))
    val locked: S = f.state("opened", List(unlock))
    f.machine(List(opened,closed,locked))
}
```

A *forward reference* error will always occur no matter how we arrange these statements. The reason is that there is no proper way to decouple the cyclic references between states and transitions.

1315 5.2. *FSM in* CASTOR

Fortunately, modeling the FSM language using CASTOR is not a problem:

```
@family trait FSM {
       @adt trait M {
         val states = ListBuffer[S]()
         class Machine
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       }
       @adt trait S {
         val trans = ListBuffer[T]()
         var name: String
         class State(var name: String)
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       }
       @adt trait T {
         class Trans(val event: String, var target: S)
       }
       @visit(M,S,T) trait Print {
1330
         type OM = String
         type OS = OM
         type OT = OM
         def machine = _.states.map{this(_)}.mkString("\n")
def state = s => s.trans.map{this(_)}.mkString(s.name+":\n","\n","")
1335
         def trans = t => t.event + " -> " + t.target.name
       }
       @visit(M,S,T) trait Step {
         type OM = String => Unit
         type OS = OM
1340
         type OT = OM
         var res: S = null
         def machine = m => event => m.states.foreach{this(_)(event)}
         def state = s => event => s.trans.foreach{this(_)(event)}
         def trans = t => event => if (event == t.event) res = t.target
1345
       }
    }
```

The actual class hierarchies of the FSM language are slightly different from what Figure 3 shows. Each class in the UML diagram is defined inside an **@adt** trait for

allowing potential variant extensions. Fields are either declared as var or val for enabling/disabling mutability.

Combined Visitors. There are two visitors defined for the FSM language, namely Print and Step. Annotated as @visit(M,S,T), both of them are combined visitors on transitions, states, and machines. Such a combined implementation is much more
 ¹³⁵⁵ compact than defining three mutually dependent visitors with distinct names. Print instantiates the output types OM, OS, OT consistently as String and implements three visit methods machine, state and trans altogether. Concretely, methods machine and state map Print to the substructures and concatenate the results with a newline. For trans, we should not call this on the target state otherwise it will not terminate. Instead, we
 ¹³⁶⁰ print out the name field on the target state only.

Imperative Visitors. The Step visitor captures a small-step execution semantics of FSM. Given an event, it goes through the structure for finding out the transition triggered by that event and returning the state that transition points to. Note that Step is also an *imperative* visitor, which instantiates the output types as String => Unit and updates

```
the field res to the found target transition. If res is still null after traversal, then no such transition exists.
```

Now we are able to model the state machine that controls doors like this:

```
import FSM._
    val door = new Machine
1370 val opened = new State("Opened")
    val closed = new State("Closed")
    val locked = new State("Locked")
    val open = new Trans("open", opened)
    val close = new Trans("close",closed)
1375 val lock = new Trans("lock",locked)
    val unlock = new Trans("unlock", closed)
    door.states += (opened,closed,locked)
    opened.trans += close
    closed.trans += (open,lock)
    locked.trans += unlock
1380
    The graph is constructed in a conventional OOP style. Unlike Object Algebras, the struc-
    ture is built top down. To decouple cyclic references, the declaration and initialization
    of the variables are separated. This is possible because unlike Object Algebras, variants
    in CASTOR are concrete classes provided with setters.
        Calling print(door) produces the following output:
1385
    Opened:
    close -> Closed
    Closed:
    open -> Opened
    lock -> Locked
1390
    Locked:
    unlock -> Closed
    Some tests on Step are:
```

```
step(door)("open")
1395 println(step.res.name) // "Opened"
step.res = null // Reset to null
step(door)("close")
```

println(step.res.name) // "Closed"

1405

Imperative visitors should be used more carefully. In the case of Step, its field res needs to be reset to null afterwards. Otherwise, the result may be wrong next time we call step.

5.3. Language Composition and Memoized Traversals

Consider unifying FSM and ARITH. The unification happens when a new kind of transition called guarded transitions is introduced. A guarded transition additionally contains a boolean term and is triggered not only by the event but also by the evaluation result of that term. Combining FSM with the GADT version of ARITH is given below:

```
@family @adts(Tm,F,S) @ops(Eval)
    trait GuardedFSM extends FSM with EvalArith {
      @adt trait T extends super[FSM].T {
        class GuardedTrans(event: String, target: State, val tm: Tm[Boolean])
1410
          extends Trans(event, target)
      3
      @visit(M,S,T) trait Print extends super[FSM].Print {
        def guardedTrans = t => trans(t) + " when " + t.tm.toString
1415
      3
      @visit(F,S,T) trait Step extends super[FSM].Step {
        def guardedTrans = t => event => if (eval(t.tm)) trans(t)(event)
      ľ
      @visit(S,T) trait Reachable {
        type OS = Unit
1420
        type OT = Unit
        val reached = collection.mutable.Set[S]()
        def state = s =>
          if (!reached.contains(s)) {
            reached += s
1425
            s.trans.foreach(this(_))
          3
        def trans = t => this(t.target)
        def guardedTrans = t => if (eval(t.tm)) this(t.target)
      }
1430
    }
```

Class GuardedTrans illustrates another form of hierarchical datatypes discussed in Section 3, which extends an existing variant Trans. The additional field tm is of type Tm[Boolean], ensuring that the evaluation result is a boolean value. To handle GuardedTrans, Print and Step are extended with an implementation of guardedTrans method. Having GuardedTrans as a subtype of Trans, we are able to partially reuse the semantics of Trans by calling the inherited trans method on a GuardedTrans instance.

Memoized Traversals. Naively traversing a graph might be inefficient because the same object may be traversed multiple times. If not dealt with carefully, the traversal may not even terminate. A more appropriate approach is to memoize the results of traversed objects and fetch the cached result when an object is traversed again. Reachable is a combined imperative visitor that finds out all reachable states for a given state. The reachable states are collected in the reached field, which is initialized as an empty mutable set. Reachable employs memoized depth-first search, which first checks
 whether the state has already been traversed. If not, the state is added to reached and

 $\begin{array}{rcl} Fam & ::= & \mathbb{Q}\mathsf{family} \ \mathbb{Q}\mathsf{adts}(\overline{D}) \ \mathbb{Q}\mathsf{ops}(\overline{V}) \ \texttt{trait} \ F \ \texttt{extends} \ \overline{F} \ \overline{Adt} \ \overline{Vis} \ \end{array}$ $\begin{array}{rcl} Adt & ::= & \mathbb{Q}\mathsf{adt} \ \texttt{trait} \ D[\overline{X}] \ \texttt{extends} \ \texttt{super}[F] \ .D[\overline{X}] \ \overline{Ctr} \ \end{array}$ $\begin{array}{rcl} Ctr & ::= & \mathbb{C}\mathsf{lass} \ C[\overline{X}] \ \texttt{extends} \ (C[\overline{T}] \ \texttt{with})? \ D[\overline{T}] \ \end{array}$ $\begin{array}{rcl} & \mathsf{object} \ C \ \texttt{extends} \ (C[\overline{T}] \ \texttt{with})? \ D[\overline{T}] \ \end{array}$ $\begin{array}{rcl} & \mathsf{vis} \ D[\overline{X}] \ \texttt{extends} \ D[\overline{T}] \ \end{array}$ $\begin{array}{rcl} Vis \ ::= & \mathbb{Q}(\mathsf{default} \ | \ \texttt{visit})(\overline{D}) \ \texttt{trait} \ V \ \texttt{extends} \ \texttt{super}[F] \ .V \ T \ & ::= \ X \ | \ D[\overline{T}] \ | \ \texttt{Int} \ | \ T \ \end{array}$

Figure 5: Syntax.

the recursion goes to the states its transitions lead to. Similarly, memoization is also applicable to functional visitors by changing reached to a mutable map.

We can build a guarded door controller by changing the *import* statement and how lock is initialized:

1450 val lock = new GuardedTrans("lock",locked,TmFalse)

Now, an opened door can no longer be locked because the guard evaluates to false: reachable(open)

```
println(reachable.reached.size) // 2
```

By setting the expression to TmTrue, the door can be locked again:

```
1455 lock.tm = TmTrue
reachable.clear // Reset to empty
reachable(open)
println(reachable.reached.size) // 3
```

6. Formalized Code Generation

¹⁴⁶⁰ In previous sections, we have shown code written with CASTOR and its corresponding generated code. In this section, we formally describe the valid Scala programs accepted by CASTOR and the transformation scheme.

6.1. Syntax

Figure 5 describes valid Scala programs accepted by CASTOR. Uppercase metavariables range over capitalized names. \overline{A} is written as a shorthand for a potentially empty sequence $A_1 \bullet \ldots \bullet A_n$, where \bullet denotes with, comma or semicolon depending on the context. (...)? denotes that ... is optional. For brevity, we ignore the syntax that is irrelevant to the transformation, such as the case modifier, constructors, fields, and methods. These parts are kept unchanged after transformation.

1470 6.2. Transformation

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Figure 6 formalizes the transformation. We use semantic brackets ($[\cdot]$) in defining the transformation rules and angle brackets (<>) for processing sequences. The transformation is given by pattern matching on the concrete syntax and is quite straightforward. One can see that processing the ARITH implementation in CASTOR (cf. Section 2.9) through Figure 6 will get back the extensible visitor implementation (cf. Section 2.7).

Here we briefly discuss some interesting cases. A trait is recognized as a *base case* if it extends nothing. Base cases have extra declarations such as accept declaration for

datatypes or val declaration for visitors. Variants declared using class, trait or object are treated differently. objects and classes have their corresponding visit methods in the visitor interface while visit methods for traits only exist in the default visitor. The extends clause for **@adt** is used in inferring the extends clause for concrete visitors.

6.3. Implementation

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CASTOR employs Scalameta [39] (version 1.8.0), a modern Scala meta-programming library, for analyzing and generating the code. The actual implementation closely follows the formalization. After parsing, the Scala source program is represented as an 1485 AST. We first check the validity of that AST with errors like annotating @adt not on a trait reported. We then generate code by analyzing the AST. Next, we build the AST with code injected. Finally, the AST is typechecked by the Scala compiler. During the process, Scala's quasiquotes are used, which allow us to analyze and rebuild the AST conveniently via the concrete syntax. 1490

7. Case Study I: Types and Programming Languages

In this section, we present a case study on modularizing the interpreters in TAPL [22]. The ARITH language and its variations are directly from or greatly inspired by the TAPL case study. TAPL are a good benchmark for examining CASTOR's capabilities of open pattern matching and modular dependencies. The reason is that core data structures of 1495 TAPL interpreters, types and terms, are modeled using algebraic datatypes; operations over types and terms are defined via pattern matching. There are a few operations that require nested patterns: small-step semantics, type equality, and subtyping relations. They all come with a default. The data structures and associated operations should be modular as new language features are introduced and combined. However, without 1500 proper support for modular pattern matching, the original implementation duplicates code for features that could be shared. With CASTOR and techniques shown in Section 2.9, we are able to refactor the non-modular implementation into a modular manner. Our evaluation shows that the refactored version significantly reduces the SLOC compared to a non-modular implementation found online. However, at the moment, improved 1505

modularity does come at some performance penalty.

7.1. Overview

An existing Scala implementation of $TAPL^2$ strictly follows the original OCaml version, which uses sealed case classes and pattern matching. The first ten languages (arith, untyped, fulluntyped, tyarith, simplebool, fullsimple, fullerror, bot, rcdsubbot and 1510 *fullsub*) are our candidates for refactoring. Each language implementation consists of 4 files: parser, syntax, core and demo. These languages cover various features including arithmetic, lambda calculus, records, fixpoints, error handling, subtyping, etc. Features are shared among these ten languages. However, such featuring sharing is achieved via duplicating code, causing problems like:

²https://github.com/ilya-klyuchnikov/tapl-scala

```
[[@family @adts(\overline{D}) @ops(\overline{V}) trait F extends \overline{F} \{ \overline{Adt} \overline{Vis} \}]] =
    trait F extends \overline{F} \{ \llbracket \overline{Adt} \rrbracket \llbracket \overline{Vis} \rrbracket \}
    object F extends F {
         \langle \text{type } D \mathbb{V} = D \mathbb{V} \text{ isit } | D \in \overline{D} \cup \overline{Adt} \rangle
         \langle \text{object } v \text{ extends } V \mid V \in \overline{V} \cup \overline{Vis} \rangle
    }
\llbracket \text{Qadt trait } D[\overline{X}] \{ \overline{Ctr} \} \rrbracket =
    type DV <:DVisit</pre>
    trait D[\overline{X}] \{ def accept(v:DV): v.OD[\overline{X}] \}
    \llbracket \overline{Ctr} \rrbracket
    trait DVisit{ _:DV =>
         type OD[\overline{X}]
         def apply[\overline{X}](x:D[\overline{X}]) = x.accept(this)
         [[Ctr]]<sub>visit</sub>
    }
    trait DDefault extends DVisit{ _:DV =>
         def d[\overline{X}] : D[\overline{X}] \implies 0D[\overline{X}]
         \llbracket \overline{Ctr} \rrbracket_{default}
    }
[[0] adt trait D extends super [F].D { <math>\overline{Ctr} } ] =
    type DV <:DVisit</pre>
    \llbracket \overline{Ctr} \rrbracket
    trait DV isit extends super [F]. DV isit { _: DV => [[\overline{Ctr}]]_{visit}}
    trait DDefault extends DVisit with \overline{\text{super}[F]}. DDefault { _: DV => [\overline{Ctr}]_{default}}
[[class C[\overline{X}] \dots]] = class C[\overline{X}] \dots \{ override def accept(v:DV) = v.c(this) \}
[[object C \dots]] = object C \dots \{ override def accept(v: DV) = v.c \}
\llbracket Ctr \rrbracket = Ctr
[[class C[\overline{X}] extends (...with)? D[\overline{T}]]]_{visit} = def c[\overline{X}]: C \Rightarrow OD[\overline{T}]
[[object C extends (... with)? D[\overline{T}]]]_{visit} = def c: 0D[\overline{T}]
\llbracket Ctr \rrbracket_{visit} = \emptyset
[[class C_1[\overline{X}] \text{ extends } C_2[\overline{T}] \dots]]_{default} = \operatorname{def} c_1[\overline{X}] = x \implies c_2(x)
\llbracket object C_1 \text{ extends } C_2[\overline{T}] \dots \rrbracket_{default} = def c_1 = c_2(C_1)
\llbracket \texttt{trait } D_1[\overline{X}] \texttt{ extends } D_2[\overline{T}] \dots \rrbracket_{default} = \texttt{def } d_1 = (\texttt{x}: D_1[\overline{X}]) \Rightarrow d_2(\texttt{x})
\llbracket \mathbb{Q}(\texttt{default} \mid \texttt{visit})(\overline{D}) \texttt{ trait } V \rrbracket =
    trait V extends D(\text{Default} | \text{Visit}) \{ \_: \overline{DV} \Rightarrow \ldots \}
    val v: V
\llbracket \mathbb{Q}(\text{default} | \text{visit})(\overline{D}) \text{ trait } V \text{ extends } \overline{\text{super}[F]} \cdot V \rrbracket =
    trait V extends \overline{D}(\text{Default} | \text{Visit}) with \overline{\text{super}[F] \cdot V} \{ \_: \overline{DV} => \dots \}
\llbracket \overline{X} \rrbracket = \langle \llbracket X \rrbracket \mid X \in \overline{X} \rangle
```

Figure 6: Transformation.



Figure 7: Simplified language/feature dependency graph.

- Inconsistent definitions. Lambdas are printed as "lambda" in all languages except for *untyped*, where lambdas are printed as "\".
- **Feature leaks.** Features introduced in the latter part of the book (e.g., System F) leak to previous language implementations such as *fullsimple*.
- ¹⁵²⁰ Our refactoring focuses on *syntax* and *core* where datatypes and associated operations are defined. Figure 7 gives a simplified high-level overview of the refactored implementation. The candidate languages are represented as gray boxes whereas extracted features/sub-languages are represented as white boxes. From Figure 7 we can see that the interactions between languages (revealed by the arrows) are quite intense. Take ARITH for example, it is a sublanguage for *tyarith*, *fulluntyped*, *fullerror*, *fullsimple* and *fullsub*. Unfortunately, without proper modularization techniques, the arisingle
- and *fullsub*. Unfortunately, without proper modularization techniques, the original implementation repeats the definition of *arith* at least five times. In the refactored implementation written with CASTOR, however, *arith* is defined only once and modularly reused in other places.

1530 7.2. Evaluation

We evaluate CASTOR by answering the following questions:

- Q1. Is CASTOR effective in reducing SLOC?
- Q2. How does CASTOR compare to EVF?
- Q3. How much performance penalty does CASTOR incur?
- ¹⁵³⁵ *Q1.* Table 2 reports the SLOC comparison results. With all the features/sublanguages extracted, implementing a candidate language with CASTOR is merely done by composing features/sublanguages. Therefore, the more features/sublanguages the candidate

Extracted	CASTOR	EVF	Language	CASTOR	EVF	Scala
bool	71	98	arith	31	33	106
extension	24	34	untyped	40	46	124
str	42	55	fulluntyped	18	47	256
let	48	47	tyarith	22	26	157
moreext	112	106	simplebool	24	38	212
nat	85	103	fullsimple	24	83	619
record	117	198	fullerror	68	105	396
top	79	86	bot	40	61	190
typed	82	138	rcdsubbot	30	39	257
varapp	40	65	fullsub	57	116	618
variant	136	161				
misc	212	172	Total	1402	1857	2935

Table 2: SLOC evaluation of TAPL interpreters

language uses, the more code CASTOR reduces. Compared to the non-modular Scala implementation, for a simple language like *arith*, the reduction rate³ is 71%; for a
feature-rich language like *fullsimple*, the reduction rate can be up to 96%. Overall, CASTOR reduces over *half* of the total SLOC with respect to the non-modular version.

Q2. Table 2 also compares CASTOR with EVF [21]. CASTOR reduces over 400 SLOC compared to EVF. As we have shown in Section 2, the reduction comes from the native support for pattern matching, generated dependency declarations, etc. More importantly, the instantiation burden for EVF is heavy if there are a lot of visitors and the dependencies are complex. In contrast, CASTOR completely removes the instantiation burden by generating companion objects automatically.

Q3. To measure the performance, we randomly generate 10,000 terms for each language and calculate the average evaluation time for 10 runs. The ScalaMeter⁴ microbenchmark framework is used for performance measurements. The benchmark programs are compiled using Scala 2.12.7, JDK version 1.8.0_211 and are executed on a MacBook Pro with 2.3 GHz quad-core Intel Core i5 processor with 8 GB memory. Figure 8 compares the execution time in milliseconds. From the figure we can see that CASTOR implementations have a 1.35x (*arith*) to 3.92x (*fullsub*) slowdown with respect to the corresponding non-modular Scala implementations. The more features a modular implementation combines, the more significant the slowdown is. Figure 9 further compares the performance of the Scala ARITH implementations discussed in Section 2. Obviously, modular implementations, the implementation based on sealed case classes is

¹⁵⁶⁰ faster than the implementation based on conventional visitors.

We believe that the performance penalty is mainly caused by method dispatching. A modular implementation typically has a complex inheritance hierarchy. Dispatching on

³Reduction rate = $\frac{\text{Scala SLOC} - \text{CASTOR SLOC}}{\text{SLOC}} \times 100\%$

⁴¹ the day of the state of the

⁴http://scalameter.github.io



Figure 8: Performance evaluation of TAPL interpreters.



Figure 9: Performance evaluation of ARITH.

- a case needs to go across that hierarchy. Thus, the more complex the hierarchy is, the worse the performance is. Another source of performance penalty might be the use of
 ¹⁵⁶⁵ functions instead of normal methods in visitors. Of course, more rigorous benchmarks need to be conducted to verify our guesses. One possible way to boost the performance is to turn TAPL interpreters into compilers via staging using the LMS framework [40]. This is currently not possible because LMS and Scalameta are incompatible in terms of the Scala compiler versions.
- *Threats to Validity.* There are two major threats to the validity of our evaluation. The first threat is that measuring conciseness by counting SLOC may not be fair especially when different languages are used. We mitigate this threat by making the code style and the maximum character-per-line consistent for each implementation. The second threat is the representativeness of the TAPL interpreters. They are small languages for teaching
- ¹⁵⁷⁵ purposes. It might still be questionable whether CASTOR scale to model larger languages that are actually used in practice. Nevertheless, TAPL interpreters have already covered a lot of core features that are available in mainstream languages.



Figure 10: Metamodel of UML Activity Diagrams (an excerpt adapted after the TTC'15 document [41]).

8. Case Study II: UML Activity Diagrams

In Section 7, we have evaluated the functional aspects of CASTOR. In this section, we evaluate the imperative aspects of CASTOR. To do so, we conduct another case study on a subset of the UML activity diagrams, which can be seen as a richer language than the FSM language discussed in Section 5. This case study examines hierarchical datatypes, imperative visitors and graphs.

8.1. Overview

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An execution model of UML activity diagrams has been proposed as one of the challenges of the Transformation Tool Contest (TTC'15).

Metamodel. Figure 10 shows the metamodel of UML activity diagrams, where *Name* denotes abstract classes and **Name** denotes concrete classes. An Activity object

represents an instance of a UML activity diagram, which contains a sequence of

- ActivityNodes and ActivityEdges. ExecutableNode and ControlNode are two intermediate types of ActivityNode for classifying nodes that perform actions or control the flow. There are several concrete nodes. InitialNode and ActivityFinalNode are the start/end of activity diagrams; DecisionNode and MergeNode are the start/end of alternative branches; ForkNode and JoinNode are the start/end of concurrent branches.
- On the other hand, OpaqueAction sequentially executes a sequence of Expressions. ActivityNodes are connected by ActivityEdges. Similar to GuardedTrans discussed in Section 5.3, a ControlFlow is a specialized ActivityEdge, which is guarded by the current BooleanValue stored in a BooleanVariable. Expressions are also organized in a hierarchical way according to their types (Boolean or Integer) and the number of operands (Unary or Binary).

Goal and Challenges. The goal is to extend this simplified metamodel of UML activity diagrams with the dynamic execution semantics. The semantics is defined by performing transitions on activity nodes step by step using an imperative style. Several *runtime concepts* need to be introduced. Adding these runtime concepts poses two modularity
 ¹⁶⁰⁵ challenges: operation extensions and *field extensions*. One example of an operation extension is execute, which is added to the Expression hierarchy for executing the calculation. One example of a field extension is a mutable boolean value running, which

is added to ActivityNode for distinguishing triggered nodes from others.

Reference Implementation. The reference implementation⁵ is written in Java with
 EMF [42]. The metamodel is described in Ecore from which Java interfaces are generated. Then semantics is encoded by defining classes that implement those interfaces using the INTERPRETER pattern [18]. The reference is non-modular because the INTERPRETER pattern facilitates adding new classes but lacks the ability to add new operations. Therefore, the reference implementation has to anticipate the operations on the meta ¹⁶¹⁵ model. Moreover, consistent with what Figure 10 shows, operators were modeled as enumerations and recognized using switch-case clauses in Java, which are closed for extensions.

Refactored Implementation. Our refactoring only focuses on the metamodel and the semantics parts. Since the original implementation is written in Java, we first port it into Scala and then refactor it using CASTOR. Figure 11 gives an overview of the refactored implementation, which consists of four CASTOR components. Concretely, we make the following changes to the ported implementation for increasing modularity:

- 1. **Separate metamodel and operations.** With CASTOR, we do not need to foresee the operations on the metamodel since operations can be modularly added afterwards. Thus, the refactored implementation separates the metamodel and operations upon it respectively in ***Model** and ***Lang**.
- 2. Expression language as an independently reusable component. Values, variables and expressions are essentially a sublanguage independent of the UML

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⁵https://github.com/moliz/moliz.ttc2015



Figure 11: Refactored implementation.

activity diagrams. Instead of defining the expression sublanguage together with UML activity diagrams within a single <code>@family</code> component, we extract its metamodel into **ExpModel** and its semantics into **ExpLang** and let **UmlModel** and **UmlLang** extend them respectively. This allows the expression sublanguage to be reused or extended individually.

- 3. Overridden methods as visitors. Methods that are overridden in the subclasses are rewritten as visitors, such as isReady and fire on ActivityNode and execute on Expression. Since only a few cases of isReady and fire are overridden whereas every case of execute is overridden, we use the default visitor (annotated as @default) for the former and the ordinary visitor (annotated as @visit) for the latter. For non-overridden methods, we move them out of a class and use an explicit argument to capture this.
- 4. **Operators as open datatypes.** Operators are refactored as **@adt** hierarchies and their semantics are given by visitors for enabling extensions. This allows new kinds of operators such as multiplication to be added later.

8.2. Evaluation

¹⁶⁴⁵ We evaluate CASTOR by answering the following questions:

- Q1. Does the refactoring preserve the behavior of the ported implementation?
- Q2. Can CASTOR solve the modularity challenges?
- Q3. How does the refactoring affect the SLOC?
- Q4. Is the performance overhead reasonable?
- *Q1.* To make sure that our refactoring does not affect the correctness of the implementation, we ran the test suite provided by the TTC'15 document. The test suite contains 6 small activity diagrams where all kinds of ActivityNodes and Expressions are covered. The refactored implementation passes all the tests in the test suite. This gives us some confidence that the refactored implementation preserves the behavior of the ported implementation.
- 1655 implementation.

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Table 3: Performance evaluation in milliseconds.							
Name	Description	INTERPRETER	CASTOR				
test ₁	1000 sequential actions	22.1	56.6				
test ₂	100 parallel branches each with 10 actions	20.7	39.8				
test ₃	Similar to test ₂ with a variable increased	22.8	39.9				

Q2. For the operation extension challenge, the answer is yes. Operations are added by defining new visitors, which are fully modular. However, CASTOR does not address the field extension challenge very well. With the current version of CASTOR, we cannot extend existing classes with additional fields while keeping their names. The workaround is to introduce subclasses of different names. For example, if we want to extend ActivityNode with a field called running, we have to define a new class called RuntimeActivityNode that extends ActivityNode with running. The drawback is that RuntimeActivityNode and ActivityNode coexist and all existing operations need to be modified for handling RuntimeActivityNode. It is possible to have an alternative design for CASTOR, which does not introduce a new name while accomplishing field extensions in CASTOR. However, this brings some other complications. Such alternative design is discussed in Section 9.2.

Q3. The SLOC of the ported version and the refactored version are 489 and 411 respectively. Surprisingly, the refactoring brings extra modularity while reducing the SLOC. One reason is that in the ported version, methods are first declared in traits and then implemented in classes while the refactored version needs no prior declarations. Another reason is that by properly using CASTOR's default visitors and combined visitors, some definitions can be shortened. For example, Execute in the refactored version is a combined visitor for Expression and 4 operators.

Q4. We reuse the test suite provided by the TTC'15 document, which includes 3 large activity diagrams for measuring the performance. Table 3 gives a simple description for each test case and the average execution time for 10 runs (measured in milliseconds) for the two implementations. The benchmark is executed using the same machine specified in Section 7. The CASTOR's implementation is around 2 to 3 times slower than the non-modular ported implementation. These results are similar to the results we get in Section 7 and further confirm that CASTOR's modular implementation introduces an

acceptable performance penalty.

Threats to Validity. One threat to the validity of the evaluation is that the test suite is very small and might not be able to find out bugs that are introduced by refactoring. Also, directly comparing a CASTOR's implementation with respect to the reference implementation may be unfair since different programming languages are used. To exclude such language-wise factor on evaluation, we compared to the ported Scala implementation. As our focus is on the semantics part, irrelevant code like parsing is ignored.

9. Limitations and Design Options

In this section, we first discuss the limitations of CASTOR, which affect some of the design decisions we made that lead CASTOR to its current form. We then discuss other design options and compromises.

9.1. Limitations

¹⁶⁹⁵ CASTOR has some limitations due to the use of metaprogramming and the restrictions from the current Scalameta library:

- Unnecessary annotations. With the current version of Scalameta, we are not able to get information from annotated parents. If parents' information were accessible, the inherited datatypes and visitors could be analyzed and @adts and @ops annotations could be eliminated.
- Boilerplate for nested composition. Lacking of parents' information also disallows automatically composing nested members. Assuming that automatic nested composition is available, Arith can be simplified as:

```
@family trait Arith extends Nat with Bool {
    @adt trait Tm { ... }
    @visit(Tm) trait Eval1 { ... }
}
```

where the extends clause is expressed only once in the family level and extends clauses for nested members such as super[Nat].Tm with super[Bool].Tm are inferred.

• **Imprecise error messages.** As CASTOR modifies the annotated programs, what the compiler reports are errors on the modified program rather than the original program. Reasoning about the error messages becomes harder as they are mispositioned and require some understanding of the generated code.

Nested Patterns. There is an alternative way of writing nested patterns. For example, tmIf can be rewritten in the following way:

```
override def tmIf = x => x.t1 match {
    case TmTrue => x.t2
    case TmFalse => x.t3
    case t1 => TmIf(this(t1),x.t2,x.t3)
}
```

Instead of directly pattern matching on an TmIf object, we capture it first using a variable x and then explicitly match on its subterm t1. For the case of tmIf, this alternative implementation is arguably less intuitive than the version we presented in Section 2.9. Nevertheless, this approach comes in handy when: 1) the object being matched contains a lot of fields and most of them are not interesting in nested patterns; 2) there are a lot of case clauses for nested patterns and repeating the top-level pattern in each case clause becomes tedious.

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^{1715 9.2.} Design Options

- Specialized Visitors. Programming with visitors can be simplified using specialized visitors. The default visitors generated by CASTOR (annotated as @default) are an instance. In fact, there are more such specialized visitors. For example, visitors can be combined with visitor combinators [43]; boilerplate for querying and transforming data structures can be eliminated by traversal templates [21]. Essentially, these specialized
- visitors can also be generated by CASTOR. Currently, only default visitors are generated because 1) in our experience they are most frequently used; 2) generating all other infrequently used specialized visitors increases the time of code generation and the size of generated code. Ideally, specialized visitors should be generated by need. Limited by current Scalameta, this is impossible for the moment.
- *Refinable Variants.* As our visitor encoding shows, the key to extensibility is capturing concrete types with bounded type members for allowing future refinements. The same idea can also be applied to variants, where the visitor method signature refers to a type member instead of a class name. By doing this, we are able to extend that class with additional fields seamlessly by covariantly refining the type member to the new class. An application of refinable variants would be guarded transitions discussed in
- Section 5.3:

class Trans(event: String, to: State, var tm: Tm[Boolean] = TmTrue)
 extends super.Trans(event, to)

Instead of adding a new variant called GuardedTrans, we refine the existing Trans. The benefit is that existing visitors that do not concern about the additional parameter tm can be unchanged. In contrast, for the case of GuardedTrans, we have to update all existing visitors with an implementation of guardedTrans. However, the downside of supporting refinable variants in CASTOR is that it brings more book-keeping burden on variants for the user. We consider the price to pay is higher than the benefit it brings.

1755 **10. Related Work**

Object-Oriented Pattern Matching. There are many attempts to bring notions similar to pattern matching into OOP. Multimethods [3, 44] allow a series of methods of the same signature to co-exist. The dispatching for these methods additionally takes the runtime type of arguments into consideration so that the most specific method is selected. Pattern matching on multiple arguments can be simulated with multimethods. However, it is unclear how to do deep patterns with multimethods. Also, multimethods significantly complicate the type system. As we have discussed in Section 2, case classes in Scala [31] provide an interesting blend between algebraic datatypes and class hierarchies. Sealed case classes are very much like classical algebraic datatypes, and

- facilitate exhaustiveness checking at the cost of a closed (non-extensible) set of variants. Open case classes support pattern matching for class hierarchies, which can modularly add new variants. However no exhaustiveness checking is possible for open case classes. Besides case classes, extractors [32] are another alternative pattern matching mechanism in Scala. An extractor is a companion object with a user-defined unapply method that
- ¹⁷⁷⁰ specifies how to tear down that object. Unlike case classes whose unapply method is automated and hidden, extractors are flexible, independent of classes but verbose. There are also proposals to extend mainstream languages with pattern matching such as

Java. JMatch [45] extends Java with pattern matching using modal abstraction. JMatch methods additionally have backward modes that can compute the arguments from a given result, serving as patterns. Follow-up work [46] extends JMatch with exhaustiveness and totality checking on patterns in the presence of subtyping and inheritance. However, it requires a non-trivial language design with the help of an SMT solver. More recent OO languages like Newspeak [47] and Grace [48] are designed with first-class pattern matching, where patterns are objects and can easily be combined. To the best of our knowledge, none of these approaches fully meet the desirable properties summarized in Section 2.1.

Modular Church-Encoded Interpreters. Solutions to the Expression Problem based on Church encodings can also be used for developing modular interpreters. Well-known techniques are Finally Tagless [11], Object Algebras [9] and Polymorphic Embedding [12]. However, these techniques do not support pattern matching or dependencies, making it hard to define operations like small-step semantics discussed in Section 2. Although Kiselyov [23] shows that operations requiring nested patterns can be rewritten as context-sensitive operations, the operations become much more convoluted. Typical workarounds on dependent operations are defining the operation together with the depen-

dencies or using advanced features like intersection types and a merge operator [49, 50]. In contrast, CASTOR allows us to implement operations that need nested patterns and/or with dependencies in a simple, modular way.

Polymorphic Variants. OCaml supports polymorphic variants [51]. Unlike traditional variants, polymorphic variant constructors are defined individually and are not tied to a particular datatype. Garrigue [52] presents a solution to the Expression Problem using polymorphic variants. To correctly deal with recursive calls, open recursion and an explicit fixed-point operator must be used properly. Otherwise, the recursion may go to the original function rather than the extended one. This causes additional work for the programmer, especially when the operation has complex dependencies. In contrast, CASTOR handles open recursion easily through OO dynamic dispatching, reducing the

burden of programmers significantly.

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Open Datatypes and Open Functions. To solve the Expression Problem, Löh and Hinze [53] propose to extend Haskell with open datatypes and open functions. Different from classic closed datatypes and closed functions, the open counterparts decentralize the definition of datatypes and functions and there is a mechanism that reassembles the pieces into a complete definition. To avoid unanticipated captures caused by classic *first-fit* pattern matching, a *best-fit* scheme is proposed, which rearranges patterns according to their specificness rather than the order (e.g. wildcards are least specific). However open datatypes and open functions are not supported in standard Haskell and

¹⁸¹⁰ more importantly, they do not support separate compilation: all source files of variants belonging to the same datatype must be available for code generation.

Data Types à la Carte (DTC). DTC [54] encodes composable datatypes using existing features of Haskell. The idea is to express extensible datatypes as a fixpoint of co-products of functors. While it is possible to define operations that have dependencies

or require nested pattern matching with DTC, the encoding becomes complicated and needs significant machinery. There is some follow-up work that tries to equip DTC with additional power. Bahr and Hvitved [55] extend DTC with GADTs [37] and automatically generates boilerplate using Template Haskell [56]. Oliveira et al. [57] use list-of-functors instead of co-products to better simulate OOP features including subtyping, inheritance, and overriding.

Language Workbenches. To reduce the engineering effort involved in software language development, language workbenches [58, 59] have been proposed. Modularity is an important concern in language workbenches for allowing existing language components to be reused in developing new languages [60]. Traditionally most of the work on language workbenches has focused on *syntactic modularity* approaches. More *semantic*

- language workbenches has focused on *syntactic modularity* approaches. More *semantic modularity* aspects such as separate compilation and modular typechecking are not well addressed. However, more recent work on language workbenches has started to incorporate semantic modularity techniques. We compare our work next, to the language workbenches that employ semantic modularization techniques. With Neverlang [61], users do not directly program with visitors. Instead, they have to use a
- erlang [61], users do not directly program with visitors. Instead, they have to use a DSL and learn specific concepts such as slice and roles. MontiCore [62] generates the visitor infrastructure from its grammar specification. To address the extensibility issue, MontiCore overrides the accept method and uses casts for choosing the right visitor for extended variants, thus is not type-safe. Also, MontiCore supports imperative style visitors only. Alex [63] also provides a form of semantic modularity based on
- 1835 style visitors only. Alex [63] also provides a form of semantic modularity based on the *Revisitor* pattern [64], which can be viewed as a combination of Object Algebras and Walkabout [65]. By moving the dispatching method from the class hierarchy to the visitor interface, the *Revisitor* pattern can work for legacy class hierarchies that do not anticipate the usage of visitors. However, the dispatching method generated by Alex
- is implemented using casts and has to be modified whenever new variants are added, thus is neither modular nor type-safe. CASTOR fully supports semantic modularity and allows users to do the development using their familiar language with a few annotations. For the moment, CASTOR still lacks much of the functionality for various other aspects of language implementations that are covered by language workbenches. Nevertheless, the modularization techniques employed by CASTOR could be useful in the context of
- language workbenches to improve reuse and type-safety of language components, in the same way that visitors are used in Neverlang and Revisitors are used in Alex.

11. Conclusion and Future Work

In this paper, we have presented CASTOR, a Scala framework for programming with extensible, generative visitors using simple annotations. Visitors written with CASTOR are type-safe, concise, exhaustive, extensible and composable. Moreover, both functional and imperative style visitors are supported. We have shown how to use CASTOR in designing a better pattern matching mechanism in an OOP context, developing modular well-typed EDSLs, doing extensible programming on graphs, etc. The effectiveness of CASTOR is validated by our case studies on TAPL interpreters and UML activity

diagrams. While CASTOR is practical and serves the purpose of programming with visitors, there are important drawbacks on such a meta-programming, library-based

approach: error reporting is imprecise; the syntax and typing of Scala cannot be changed to enforce certain restrictions. In future work, we would like to design a language with a better surface syntax that supports first-class visitors. Another direction of future work is to grow CASTOR into a language workbench by additionally supporting syntax and

Acknowledgement

associated tools development.

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References

- [1] P. Wadler, The Expression Problem, Email, discussion on the Java Genericity mailing list (Nov. 1998).
- [2] O. L. Madsen, B. Moller-Pedersen, Virtual classes: A powerful mechanism in object-oriented programming, in: Proceedings on Object-oriented Programming Systems, Languages and Applications, OOPSLA '89, 1989. doi:10.1145/ 74877.74919.
 - [3] C. Chambers, Object-oriented multi-methods in cecil, in: Proceedings of the European Conference on Object-Oriented Programming, ECOOP '92, 1992. doi: 10.5555/646150.679216.
 - [4] E. Ernst, Family polymorphism, in: Proceedings of the 15th European Conference on Object-Oriented Programming, ECOOP '01, 2001.
 - [5] G. Bracha, W. Cook, Mixin-based inheritance, in: Proceedings of the European Conference on Object-oriented Programming on Object-oriented Programming Systems, Languages, and Applications, OOPSLA/ECOOP '90, 1990.
 - [6] A. Moors, F. Piessens, M. Odersky, Generics of a higher kind, in: Proceedings of the 23rd ACM SIGPLAN Conference on Object-oriented Programming Systems Languages and Applications, OOPSLA '08, 2008. doi:10.1145/1449764. 1449798.
 - [7] K. K. Thorup, Genericity in java with virtual types, in: European Conference on Object-Oriented Programming, 1997.
 - [8] S. Ducasse, O. Nierstrasz, N. Schärli, R. Wuyts, A. P. Black, Traits: A mechanism for fine-grained reuse, ACM Trans. Program. Lang. Syst. (2006). doi:10.1145/ 1119479.1119483.
- 1890

1875

1880

1885

[9] B. C. d. S. Oliveira, W. R. Cook, Extensibility for the masses: Practical extensibility with object algebras, in: Proceedings of the 26th European Conference on Object-Oriented Programming, 2012.

- [10] B. C. d. S. Oliveira, Modular visitor components, in: Proceedings of the 23rd
 European Conference on Object-Oriented Programming, 2009.
 - [11] J. Carette, O. Kiselyov, C.-c. Shan, Finally tagless, partially evaluated: Tagless staged interpreters for simpler typed languages, Journal of Functional Programming 19 (5) (2009) 509–543.
 - [12] C. Hofer, K. Ostermann, T. Rendel, A. Moors, Polymorphic embedding of dsls, in: Proceedings of the 7th International Conference on Generative Programming and Component Engineering, GPCE '08, 2008.

- [13] A. Church, An unsolvable problem of elementary number theory, American journal of mathematics 58 (2) (1936) 345–363.
- [14] D. Scott, A system of functional abstraction, Unpublished manuscript (1963).
- ¹⁹⁰⁵ [15] R. Hinze, Generics for the Masses, Journal of Functional Programming 16 (4-5) (2006) 451–483. doi:10.1017/S0956796806006022.
 - [16] B. C. d. S. Oliveira, R. Hinze, A. Löh, Extensible and Modular Generics for the Masses, in: Trends in Functional Programming, 2006.
- [17] B. C. d. S. Oliveira, J. Gibbons, Typecase: A design pattern for type-indexed functions, in: Proceedings of the 2005 ACM SIGPLAN Workshop on Haskell, Haskell '05, 2005.
 - [18] E. Gamma, R. Helm, R. Johnson, J. Vlissides, Design Patterns : Elements of Reusable Object-Oriented Software, Addison-Wesley, 1994.
- [19] P. Buchlovsky, H. Thielecke, A type-theoretic reconstruction of the visitor pattern,
 Electron. Notes Theor. Comput. Sci. 155 (2006) 309–329. doi:10.1016/j.
 entcs.2005.11.061.
 - [20] J. Gibbons, Origami programming, 2003, pp. 41-60. URL http://www.comlab.ox.ac.uk/oucl/work/jeremy.gibbons/ publications/origami.pdf
- [21] W. Zhang, B. C. d. S. Oliveira, Evf: An extensible and expressive visitor framework for programming language reuse, in: 31st European Conference on Object-Oriented Programming, Leibniz International Proceedings in Informatics (LIPIcs), 2017. doi:10.4230/LIPIcs.ECOOP.2017.29.
 - [22] B. C. Pierce, Types and programming languages, MIT press, 2002.
- [23] O. Kiselyov, Typed tagless final interpreters, in: Generic and Indexed Programming, Springer, 2012, pp. 130–174.
 - [24] T. Millstein, C. Bleckner, C. Chambers, Modular typechecking for hierarchically extensible datatypes and functions, ACM Trans. Program. Lang. Syst. 26 (5) (Sep. 2004).

- ¹⁹³⁰ [25] W. Zhang, B. C. d. S. Oliveira, Pattern matching in an open world, in: Proceedings of the 17th ACM SIGPLAN International Conference on Generative Programming: Concepts and Experiences, 2018. doi:10.1145/3278122.3278124.
 - [26] R. Milner, M. Tofte, R. Harper, D. Macqueen, The definition of standard ml-revised (1997).
- ¹⁹³⁵ [27] S. P. Jones, Haskell 98 language and libraries: the revised report, Cambridge University Press, 2003.
 - [28] B. Meyer, K. Arnout, Componentization: the visitor example, Computer 39 (7) (2006) 23–30.
 - [29] T. Pati, J. H. Hill, A survey report of enhancements to the visitor software design pattern, Software: Practice and Experience 44 (6) (2014) 699–733.
 - [30] R. C. Martin, The Principles, Patterns, and Practices of Agile Software Development, Prentice Hall, 2002.
 - [31] M. Odersky, P. Altherr, V. Cremet, B. Emir, S. Maneth, S. Micheloud, N. Mihaylov, M. Schinz, E. Stenman, M. Zenger, An overview of the scala programming language, Tech. rep. (2004).
 - [32] B. Emir, M. Odersky, J. Williams, Matching objects with patterns, in: European Conference on Object-Oriented Programming, 2007.
 - [33] M. Zenger, M. Odersky, Extensible algebraic datatypes with defaults, in: Proceedings of the Sixth ACM SIGPLAN International Conference on Functional Programming, 2001.
 - [34] M. Odersky, M. Zenger, Independently extensible solutions to the expression problem, in: The 12th International Workshop on Foundations of Object-Oriented Languages, 2005.
- [35] C. Hofer, K. Ostermann, Modular domain-specific language components in scala,
 in: Proceedings of the Ninth International Conference on Generative Programming and Component Engineering, GPCE '10, 2010.
 - [36] M. E. Nordberg III, Variations on the visitor pattern, in: PLoP'96 Writer's Workshop, Vol. 154, 1996.
 - [37] H. Xi, C. Chen, G. Chen, Guarded recursive datatype constructors, in: Proceedings of the 30th ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, POPL '03, 2003.
 - [38] F. Pfenning, C. Elliott, Higher-order abstract syntax, in: Proceedings of the ACM SIGPLAN 1988 Conference on Programming Language Design and Implementation, PLDI '88, 1988. doi:10.1145/53990.54010.
- ¹⁹⁶⁵ [39] E. Burmako, Unification of compile-time and runtime metaprogramming in scala, Ph.D. thesis, EPFL (2017).

1945

1950

- [40] T. Rompf, M. Odersky, Lightweight Modular Staging: A Pragmatic Approach to Runtime Code Generation and Compiled DSLs, in: In GPCE, 2010.
- [41] T. Mayerhofer, M. Wimmer, The ttc 2015 model execution case., in: TTC@ STAF, 2015, pp. 2–18.
 - [42] D. Steinberg, F. Budinsky, E. Merks, M. Paternostro, EMF: eclipse modeling framework, Pearson Education, 2008.
 - [43] J. Visser, Visitor combination and traversal control, in: Proceedings of the 16th ACM SIGPLAN Conference on Object-oriented Programming, Systems, Languages, and Applications, OOPSLA '01, 2001. doi:10.1145/504282.504302.

- [44] C. Clifton, G. T. Leavens, C. Chambers, T. Millstein, Multijava: Modular open classes and symmetric multiple dispatch for java, in: ACM Sigplan Notices, Vol. 35, ACM, 2000, pp. 130–145.
- [45] J. Liu, A. C. Myers, Jmatch: Iterable abstract pattern matching for java, in: PADL, 2003.
 - [46] C. Isradisaikul, A. C. Myers, Reconciling exhaustive pattern matching with objects, in: Proceedings of the 34th ACM SIGPLAN Conference on Programming Language Design and Implementation, PLDI '13, 2013.
 - [47] F. Geller, R. Hirschfeld, G. Bracha, Pattern Matching for an object-oriented and dynamically typed programming language, no. 36, Universitätsverlag Potsdam, 2010.
 - [48] M. Homer, J. Noble, K. B. Bruce, A. P. Black, D. J. Pearce, Patterns as objects in grace, in: Proceedings of the 8th Symposium on Dynamic Languages, DLS '12, New York, NY, USA, 2012, pp. 17–28.
- [49] B. C. d. S. Oliveira, T. v. d. Storm, A. Loh, W. R. Cook, Feature-oriented programming with object algebras, in: Proceedings of the 27th European Conference on Object-Oriented Programming, 2013.
 - [50] T. Rendel, J. I. Brachthäuser, K. Ostermann, From object algebras to attribute grammars, in: Proceedings of the 2014 ACM International Conference on Object-Oriented Programming Systems Languages and Applications, 2014.
 - [51] J. Garrigue, Programming with polymorphic variants, in: ML Workshop, 1998.
 - [52] J. Garrigue, Code reuse through polymorphic variants, in: Workshop on Foundations of Software Engineering, 2000.
 - [53] A. Löh, R. Hinze, Open data types and open functions, in: Proceedings of the 8th ACM SIGPLAN international conference on Principles and practice of declarative programming, 2006.
 - [54] W. Swierstra, Data types à la carte, Journal of functional programming 18 (4) (2008) 423–436.

1985

1995

- [55] P. Bahr, T. Hvitved, Compositional data types, in: Proceedings of the seventh ACM SIGPLAN workshop on Generic programming, ACM, 2011, pp. 83–94.
 - [56] T. Sheard, S. P. Jones, Template meta-programming for haskell, in: Proceedings of the 2002 ACM SIGPLAN workshop on Haskell, 2002.
 - [57] B. C. d. S. Oliveira, S.-C. Mu, S.-H. You, Modular reifiable matching: A list-offunctors approach to two-level types, in: Proceedings of the 2015 ACM SIGPLAN Symposium on Haskell, Haskell '15, 2015.
 - [58] M. Fowler, Language workbenches: The killer-app for domain specific languages (2005).

URL http://martinfowler.com/articles/languageWorkbench.html

- [59] S. Erdweg, T. Van Der Storm, M. Völter, M. Boersma, R. Bosman, W. R. Cook,
 A. Gerritsen, A. Hulshout, S. Kelly, A. Loh, et al., The state of the art in language workbenches, in: International Conference on Software Language Engineering, 2013.
 - [60] B. Combemale, J. Kienzle, G. Mussbacher, O. Barais, E. Bousse, W. Cazzola, P. Collet, T. Degueule, R. Heinrich, J.-M. Jézéquel, et al., Concern-oriented language development (cold): Fostering reuse in language engineering, Computer Languages, Systems & Structures 54 (2018) 139–155.
 - [61] E. Vacchi, W. Cazzola, Neverlang: A framework for feature-oriented language development, Computer Languages, Systems & Structures 43 (2015) 1–40.
- [62] R. Heim, P. M. S. Nazari, B. Rumpe, A. Wortmann, Compositional language engineering using generated, extensible, static type-safe visitors, in: European Conference on Modelling Foundations and Applications, 2016.
 - [63] M. Leduc, T. Degueule, B. Combemale, Modular language composition for the masses, in: Proceedings of the 11th ACM SIGPLAN International Conference on Software Language Engineering, 2018.
- [64] M. Leduc, T. Degueule, B. Combemale, T. Van Der Storm, O. Barais, Revisiting visitors for modular extension of executable dsmls, in: 2017 ACM/IEEE 20th International Conference on Model Driven Engineering Languages and Systems (MODELS), 2017.
 - [65] J. Palsberg, C. B. Jay, The essence of the visitor pattern, in: Proceedings of the 22nd International Computer Software and Applications Conference, 1998.

2005

2010

- 2020